Thermodynamics of Cr(VI) adsorption on strong alkaline anion exchange fiber

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Received 19 October 2011; accepted 14 December 2011

Abstract: Removal of Cr(VI) from aqueous solution by strong alkaline anion exchange fiber (SAAEF) was achieved using batch adsorption experiments. The effect of contact time, initial Cr(VI) concentration and pH was investigated. The results showed that the maximum adsorption capacity of SAAEF was 187.7 mg/g at pH=1.0. The adsorption capacity increased with Cr(VI) concentration but decreased with pH value when pH>1.0. Adsorption isotherms at various temperatures were obtained. Langmuir, Freundlich, Dubinin-Radushkevich and Temkin models were adopted and the equilibrium data fitted best with the Langmuir isotherm. The constants of these models indicated that the adsorption process involved both chemisorption and physisorption. The values of thermodynamic parameters, including $\Delta H$, $\Delta G$ and $\Delta S$, suggested that the adsorption of Cr(VI) on SAAEF was a spontaneous, entropy-driven and endothermic process. $Q_{(iso)}$ was not a constant value, which indicated an inhomogenous energy distribution on SAAEF.

Key words: strong alkaline anion exchange fiber; hexavalent chromium; isotherm; thermodynamics; chemisorption; physisorption

1 Introduction

Aquatic pollution by heavy toxic metals is a serious environmental problem. Among all the heavy metal ions, Cr(VI) is considered more hazardous to biological systems due to its mutagenic and carcinogenic properties [1]. Cr(VI) could do damage to liver, kidney circulatory and nerve tissues while Cr (III) is much less toxic. Industry discharge of Cr(VI), including mining, textile dyeing, steel fabrication, electroplating, paints and pigments, leather tanning, and chromate preparation [2], is the main source of Cr(VI) pollutants in the last few years [3]. The permissible limit for Cr(VI) is 0.5 mg/L in industrial wastewater [4] while the value is 0.05 mg/L for drinking water by World Health Organization [5].

The conventional method of Cr(VI) removal is the combination of chemical reduction and chemical precipitation. Cr(III) precipitates as Cr(OH)$_3$ at high pH value following the reduction of Cr(VI) to Cr (III). The reductants usually used are FeSO$_4$, NaHSO$_3$ and Na$_2$SO$_3$ [6,7]. The residual metal sludge generated easily brings secondary pollution and needs high cost to disposal [8]. Filtration, adsorption, photocatalytic reduction, electrolysis, liquid membrane, ion exchange [9,10], and biological processes based on physical, chemical and biological mechanisms are advisable for Cr(VI) removal. Adsorption is an economic and cost-effective technique with variety of adsorbent materials. Active carbon is the common adsorbent for Cr(VI) removal [2,6,11,12]. A lot of low cost biosorbents including pomace [13], chitosan [8,14], seed pods [15] and some industry wastes have also been studied as Cr(VI) absorbents[16,17]. Low efficiency is the main drawback of adsorption. Membrane, electrochemical treatment performs high efficiency but needs much operational capital. Ion exchange method has many advantages, such as selectivity, recovery of metal value, less sludge volume produced and the meeting of strict discharge specifications [18]. In ion exchange systems, polymeric ion exchange resin (IER) is usually employed. However, IER could be easily poisoned by some organic or inorganic compounds when the pores were clogged by the colloids in the treated solution.

Strong alkaline anion exchange fiber (SAAEF) is a new kind of fabric absorption and separation material. It has higher adsorption/desorption rate and better antipollution ability than ion exchange resin due to the
location of function groups [19]. After a number of saturation/regeneration cycles, the fiber is still suitable to further utilization compared with the short life span of IER, which reduces the industrial cost. Besides, there are many application forms of fiber, such as yarn, woven fabric and non-woven fabric. SAAEF has been applied to metal recovery, gas purification and separation, extraction and separation of rare earth and radioactive elements, water purification [20]. Currently, it has also been proposed to use ion-exchange fiber in medical and pharmaceutical applications [21].

In this study, SAAEF was used to the removal of Cr(VI) from aqueous solution. FT-IR spectra before and after adsorption were compared. Factors that affect the adsorption including contact time, initial concentration and pH value were evaluated. Equilibrium isotherm models were applied to obtaining the thermodynamic property and mechanism of Cr(VI) adsorption on SAAEF. Besides, thermodynamic parameters $\Delta H$, $\Delta G$, $\Delta S$ and $Q_{(iso)}$ were calculated.

2 Experimental

2.1 Materials

Strong alkaline anion exchange fiber was synthesized by grafting copolymerization of styrene and divinylbenzene onto polypropylene fiber induced by $^{60}$Co $\gamma$-ray co-irradiation followed by chloromethylation and amination [22]. Before the usage, SAAEF was converted to Cl$^-$ type. The chemical structure of SAAEF is shown in Fig. 1.

![Fig. 1 Chemical structure of SAAEF](image)

Aqueous solution of Cr(VI) was prepared by dissolving potassium dichromate (K$_2$Cr$_2$O$_7$) in distilled water. 1,5-diphenylcarbazide (C$_{13}$H$_{14}$N$_4$O), acetone, sulfuric acid (95%−98%), and phosphoric acid (≥85%) were used in the analysis of Cr(VI). The initial pH value of Cr(VI) solution was adjusted with sodium hydroxide (NaOH) hydrochloric acid (36%). All reagents used were of chemical grade.

2.2 Equipments

 Equipments included electronic scale (AR2140 Ohaus), precision acidity meter (PHS-25 Jingke), mechanical pipettor (20−200 $\mu$L Biohit), UV-visible spectrophotometer (725P Apl), water batch oscillator (SHA-B) and Fourier transform infrared spectrometer (TENSOR 27 Bruker).

2.3 Analytical method

The concentration of Cr(VI) was determined by UV-visible spectroscopy using 1,5-diphenylcarbazide as the complexing agent at the wavelength of 540 nm (GB 7467—87). The linear equation of standard curve could be described as

$$A = 0.7749 + 0.0024$$

(1)

where $A$ is the absorbance of the purple colored solution, and $c$ is the concentration of Cr(VI). The correlation coefficient $R^2=0.9999$.

2.4 Adsorption experiment

Adsorption experiments were carried out under batch mode. 20 mL of Cr(VI) aqueous solution with particular initial concentration and pH value was placed in a set of 50 mL glass conical flasks, respectively. Fixed mass of SAAEF was added to the adsorbent solutions. In a water batch oscillator, the mixture of Cr(VI) and SAAEF was agitated at an agitation speed of 120 r/min under a constant temperature for a certain time. The aqueous solution was sampled at predetermined time intervals.

Adsorption capacities at time $t$, $q_t$, and equilibrium, $q_e$, are expressed respectively as

$$q_t = \frac{(c_0 - c_t)V}{m}$$

(2)

$$q_e = \frac{(c_0 - c_e)V}{m}$$

(3)

where $c_0$, $c_t$ and $c_e$ are Cr(VI) the concentrations of original, residual and equilibrium Cr(VI) ion solution, respectively; $V$ is the volume of solution; $m$ is the mass of SAAEF.

2.5 Adsorbent characterization

The characterization of the adsorbent before and after Cr(VI) adsorption was investigated with a Fourier transform infrared spectrocope (FT-IR) in the wave number range of 500−4000 cm$^{-1}$.

3 Results and discussion

3.1 Characterization of SAAEF

In the FT-IR spectra, 4000−1500 cm$^{-1}$ scope is the characteristic frequency zone, making an assay of some main functional groups, such as O−H, C−H, N−H, C=C, C=N, N=N, C=O, C≡N. The zone where
wave numbers below 1500 cm\(^{-1}\) called fingerprint region shows some signal bonds and the adsorption peaks are weak. This region reflects subtle changes in molecular structure [23]. The FT-IR spectrum change before and after the adsorption of Cr(VI) on SAAEF is shown in Fig. 2.

The FT-IR spectra in the characteristic frequency region were almost the same before and after the adsorption, indicating that the main functional groups on SAAEF did not change. The main functional groups and the corresponding infrared bands are shown in Table 1. The spectrum change after adsorption appeared in the fingerprint region. The characteristic sorption peaks at 925, 892 and 859 cm\(^{-1}\) became strong after the adsorption. This could be explained by the fact that N—C stretch vibration was strengthened after the ion exchange of Cl\(^{-}\) to Cr(VI) ions, making the corresponding bands to be strong.

<table>
<thead>
<tr>
<th>IR peak in Fig. 2</th>
<th>Adsorption band/cm(^{-1}) Before adsorption</th>
<th>Adsorption band/cm(^{-1}) After adsorption</th>
<th>Assignment</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>3454</td>
<td>3442</td>
<td>Bonded —OH groups</td>
</tr>
<tr>
<td>2</td>
<td>3026</td>
<td>3025</td>
<td>Benzene C—H stretching</td>
</tr>
<tr>
<td>3</td>
<td>2923</td>
<td>2920</td>
<td>—CH(_2) groups connected to benzene ring</td>
</tr>
<tr>
<td>4</td>
<td>1632, 1513, 1492</td>
<td>1631, 1512, 1471</td>
<td>Benzene ring skeleton stretching</td>
</tr>
<tr>
<td>5</td>
<td>1426, 1378, 1425, 1375</td>
<td>1425, 1375</td>
<td>—CH(_3) groups</td>
</tr>
</tbody>
</table>

### 3.2 Adsorption curve

Adsorption curve expressed in terms of adsorption capacity \((q_e)\) of SAAEF as a function of time \((t)\) is adopted to determine the time of equilibrium. The adsorption curve of SAAEF was carried out (20 mL 483.8 mg/L \(K_2Cr_2O_7\), 0.0498 g SAAEF, 294 K, 120 r/min). The results in Fig. 3 show that the adsorption of Cr(VI) onto SAAEF was rather quick and adsorption equilibrium between \(K_2Cr_2O_7\) solution and SAAEF almost finished within 10 min, and the increase of Cr(VI) uptake was subtle after 10 min. The adsorption amount of Cr(VI) ions reached a maximum of 187.8 mg/g after 24 h.

![Fig. 2 FT-IR spectra of SAAEF before Cr(VI) adsorption (a) and after Cr(VI) adsorption (b)](image)

![Fig. 3 Effect of time on adsorption](image)

### 3.3 Effect of Cr(VI) concentration

The effect of Cr(VI) concentration on adsorption was investigated at the chromium concentration of 10–600 mg/L. 0.05 g (±0.0005 g) SAAEF was added to the solution at 303 K. The mixture was agitated at 120 r/min until the adsorption equilibrium.

Figure 4 shows that the adsorption capacity of Cr(VI) increased with increasing initial Cr(VI) concentration and the maximum adsorption capacity of Cr(VI) was 174. 2 mg/g. This could be explained by the fact that increasing the concentration gradient was attributed to the efficiency of Cr(VI) adsorption. Besides, \(q_e\) and \(c_0\) fitted a good linear relationship before the platform of adsorption capacity appeared.

![Fig. 4 Effect of Cr(VI) concentration on adsorption](image)
3.4 Effect of pH

The pH value of solution is one of the most important process parameters for the adsorption of metal, especially for the metals whose speciation is governed by the solution acidity. Some experiments were carried out to examine the influence of initial pH on the adsorption of Cr(VI) ions with 600.0 mg/L solutions and 0.05 g (±0.0005 g) SAAEF at 313 K and 120 r/min agitation for 2 h. The initial pH value of the solution was adjusted from 0.50 to 6.50 with HCl or KOH solution.

Figure 5 shows the effect of pH on the Cr(VI) adsorption. SAAEF reached a maximum value of adsorption capacity at pH=1.00. A major drop is observed in removal extent as pH value increases from 1.00 to 6.50. The adsorption capacity of Cr(VI) reduces from 187.7 mg/g to 171.6 mg/g as the pH value increases from 1.00 to 4.00 while the adsorption capacity is stable at about 171.0 mg/g in the pH range of 4.00−5.50. When the pH value is higher than 5.5, the adsorption capacity sharply decreases to 137.8 mg/g at pH=6.50.

When the pH value is lower than 1.00, Cr(VI) is present predominantly as H₂Cr₂O₇. This molecular form is hindrance to the adsorption based on the fact that the adsorption mechanism of Cr(VI) by SAAEF is ion exchange. With increasing pH value in the range of 1.00−3.00, there exists a mixture of Cr(VI) speciation, including HCrO₄⁻, HCr₂O₇⁻, Cr₃O₁₀²⁻ and Cr₄O₁₃²⁻, and decreasing the pH value results in the formation of more polymerised chromium oxide species [24]. Fewer active sites on SAAEF are needed to finish the ion exchange with more polymerised chromium oxide species with the same electric charge, leading to a higher level of Cr(VI) ion uptake. In the pH value range of 3.00−6.00, the speciation of Cr(VI) is stable at HCrO₄⁻ and Cr₂O₇²⁻ [25], which needs one active site on SAAEF to finish one corresponding Cr(VI) removal. This is in accordance with the experiment data at stable adsorption capacity of 171.0 mg/g. The sharp decrease of adsorption capacity at even higher pH value (pH>5.50) could be explained by the dual competition of the anions to be adsorbed on SAAEF of which OH⁻ predominates as the availability of OH⁻ increased.

3.5 Isotherm studies

Equilibrium isotherms at different temperatures for Cr(VI) adsorption on SAAEF experiments were performed at pH=3.0 (20 mL initial Cr(VI) solution of 393.1 mg/L, 0.0400, 0.0430, 0.0450, 0.048, 0.0500, 0.0550, 0.0600, 0.0700, 0.0800 or 0.0900 mg SAAEF, respectively). Figure 6 shows the equilibrium isotherms for Cr(VI) adsorption on SAAEF.

![Fig. 6 Adsorption isotherms of Cr(VI)](image)

It can be seen that the isotherm rises in the initial stage with a higher slope at low ρₑ and qₑ values until the plateau appears. All the isotherms at various temperatures are close to each other. This indicates that temperature is not a critical factor to Cr(VI) adsorption. The Cr(VI) uptake decreased with temperature. This implies an exothermic process of Cr(VI) adsorption on SAAEF in a temperature range of 293−323 K.

Several adsorption isotherm models, such as Langmuir, Freundlich, Dubinin-Radushkevich and Temkin model, were employed to describe the adsorption equilibrium between SAAEF and Cr(VI) ion.

3.5.1 Langmuir model

The Langmuir model [26] could be described as

\[ q_e = \frac{q_m k_L c_e}{1 + k_L c_e} \]  

where \( c_e \) is the equilibrium concentration of Cr(VI); \( q_e \) and \( q_m \) are the equilibrium adsorption amount of Cr(VI) and the saturated monolayer adsorption capacity of Cr(VI) on SAAEF, respectively; \( k_L \) is an adsorption equilibrium constant depending on the affinity of binding sites. Equation (5) is transformed to the linear form of the Langmuir equation:
Figure 7 displays the fitting lines of the Langmuir equation in all cases. \(q_m\) and \(k_L\) at each temperature were obtained by the linear regression method and presented in Table 2. The high correlation coefficients \(R^2 > 0.998\) and the value of \(q_m\) calculated of 178.6 mg/g, which corresponds to the experimental value of 176.7 mg/g, suggest that Langmuir model fitted the sorption data well and the Langmuir equation could be used as the thermodynamic model of Cr(VI) adsorption on SAAEF.

Cr(VI) adsorption is a monolayer adsorption process, indicating the chemisorption property between Cr(VI) ion and the active sites on SAAEF. Both \(q_m\) and \(k_L\) decreased in order of an increase in temperature. This could be explained by the fact that the attraction potential between \(\text{Cr}_2\text{O}_7^{2-}\) and active sites on SAAEF was getting lower, leading to \(k_L\) reduction and less Cr(VI) uptake.

Another equilibrium parameter or a separation factor, \(R_L\), expresses the essential features of a Langmuir isotherm. The relationships between them are:

\[ R_L > 1, \text{ unfavorable adsorption; } R_L = 1, \text{ linear adsorption; } 0 < R_L < 1, \text{ favorable adsorption; } R_L = 0, \text{ irreversible adsorption} \quad [27]. \]

\(R_L\) is defined as

\[ R_L = \frac{1}{1 + k_Lc_0} \quad (6) \]

where \(k_L\) is the Langmuir constant and \(c_0\) is the initial concentration. The calculated values of \(k_L\) are included in Table 2. The values of \(R_L\) at all temperature are found to be in the range of 0–1, indicating a favorable adsorption of Cr(VI) adsorption on SAAEF and a good performance of SAAEF for the removal of Cr(VI).

### 3.5.2 Freundlich model

The freundlich model \([28]\) based on multi-molecular layer adsorption on an energy heterogeneous surface is an empirical equation and expressed as

\[ q_e = k_Fc_e^{1/n} \quad (7) \]

The linear form is

\[ \ln q_e = \frac{1}{n}\ln c_e + \ln k_F \quad (8) \]

where \(k_F\) and \(n\) are the Freundlich constants related to adsorption capacity and intensity, respectively. The slope and the intercept of the line give the values of \(k_F\) and \(n\) respectively. The maximum sorption capacity \((q_m)\) can be also obtained by the following equation:

\[ q_m = k_Fc_0^{1/n} \quad (9) \]

where \(c_0\) is the initial concentration of solution. The values of \(k_F\), \(n\), \(q_m\) and the correlation coefficients of fitting lines are given in Table 2.

### Table 2 Adsorption equilibrium constants obtained from Langmuir and Freundlich isotherms in adsorption of Cr(VI) onto SAAEF

<table>
<thead>
<tr>
<th>Temperature/K</th>
<th>(k_L/10^{-3})</th>
<th>(q_m/(\text{mg g}^{-1}))</th>
<th>(R^2)</th>
<th>(k_F)</th>
<th>(n)</th>
<th>(q_m^0/(\text{mg g}^{-1}))</th>
<th>(R^2)</th>
</tr>
</thead>
<tbody>
<tr>
<td>293</td>
<td>1363</td>
<td>178.6</td>
<td>0.9997</td>
<td>109.0</td>
<td>6.350</td>
<td>279.3</td>
<td>0.7729</td>
</tr>
<tr>
<td>303</td>
<td>1369</td>
<td>171.8</td>
<td>0.9997</td>
<td>104.2</td>
<td>6.433</td>
<td>263.8</td>
<td>0.7257</td>
</tr>
<tr>
<td>313</td>
<td>911.6</td>
<td>170.0</td>
<td>0.9988</td>
<td>98.61</td>
<td>6.392</td>
<td>251.1</td>
<td>0.6140</td>
</tr>
<tr>
<td>323</td>
<td>816.3</td>
<td>157.5</td>
<td>0.9990</td>
<td>97.30</td>
<td>5.656</td>
<td>279.8</td>
<td>0.6281</td>
</tr>
</tbody>
</table>

The significant decrement of \(k_F\), \(n\) and \(q_m\) with the rise in temperature shows the evidence of an exothermic process and values of \(n\) larger than 1 show the favorability of adsorption, which agrees with the results from the Langmuir model. However, the maximum \(q_m\) value of 279.8 mg/g does not conform to the experimental data and the related coefficient \(R^2\) is lower. Therefore, the experiment data were not well described by the Freundlich equation, which proved that the adsorption of Cr(VI) on SAAEF is not a multi-molecular layer physical adsorption process.

### 3.5.3 Dubinin-Radushkevich model

Dubinin-Radushkevich \([29]\) equation is another important isotherm model, and the equation is expressed as follows:

\[ q_e = q_m\exp(-ke^2) \quad (10) \]

After logarithmic transformation, the linear form is

\[ \ln q_e = \ln q_m - kke^2 \quad (11) \]

where \(q_m\) is the maximum adsorption capacity; \(k\) is a constant related to the energy of adsorption; \(e\) is the Polanyi potential, which is calculated from the following equation:
\[ e = RT \ln(1 + \frac{1}{c_e}) \]  

(12)

where \( c_e \) is the retained concentration of solution; \( R \) is the mole gas constant; \( T \) is the thermodynamic temperature.

The mean free energy of adsorption \( (E) \) is calculated using the value of \( k \) according to Eq. (12).

\[ E = (2k)^{0.5} \]  

(13)

The plot of \( \ln q_e \) versus \( \varepsilon^2 \) is displayed in Fig. 8. The obtained coefficients of determination \( (R^2) \) for the Dubinin-Radushkevich model confirmed a good fit of equilibrium data. The constants \( k, q_m \) and \( E \) are tabulated in Table 3.

The maximum value of \( q_m \) regressed from the lines was 168.6 mg/g, which was in proximity with the experimental \( q_m \) value of 176.7 mg/g, indicating the applicability of the Dubinin-Radushkevich model to the adsorption of Cr(VI) on SAAEF. The value of \( E \) depicted the type of adsorption. When its value is between 8 and 16 kJ/mol, it is an ion exchange adsorption, while it is a physisorption process when \( E \) is lower than \(-40 \) kJ/mol. The maximum value of \( E \) obtained was 1.741 kJ/mol. This suggests that the adsorption of Cr(VI) on SAAEF is not only chemisorption of ion exchange, but also physical adsorption. It is a combination of chemisorption and physical adsorption of Cr(VI) removal.

3.5.4 Temkin model

Temkin model [30] had been established ground on the effects of indirect interactions among adsorbates on adsorption isotherms. The equation of Temkin model is

\[ q_e = \frac{RT}{b} \ln A c_e \]  

(14)

The linear form of Eq. (14) is

\[ q_e = B \ln A + B \ln c_e \]  

(15)

where \( B = RT/b; T \) is the thermodynamic temperature; \( R \) is the mole gas constant \((8.314 \text{ J/(mol·K)})\); \( A \) is the equilibrium binding constant corresponding to the maximum binding energy; \( b \) is the Temkin constant related to the heat of adsorption.

The constants of the Temkin model were obtained as shown in Table 3. In an ion exchange mechanism, the typical bonding energy range is \( 8–16 \) kJ/mol while the value of it is less than \(-40 \) kJ/mol in the physisorption processes. The values of \( b \) is about 0.10 kJ/mol at all temperatures, which indicates that the adsorption of Cr(VI) on SAAEF involved both chemisorption and physisorption. This is consistent with the result from the Langmuir model. Besides, the values of the Temkin isotherm constant decreased with the temperature, indicating the exothermic nature of Cr(VI) adsorption. However, the related coefficient \( R^2 \) is lower compared with the other models.

3.6 Thermodynamic study

The thermodynamic study of Cr(VI) adsorption on SAAEF is critical to the adsorption mechanism. The values of thermodynamic parameters were calculated.

3.6.1 Isometric heat of adsorption \( Q_{(iso)} \)

\( Q_{(iso)} \) is adopted to measure the strength of adsorption. It is the amount of heat release during the adsorption process under a constant temperature. The value of \( Q_{(iso)} \) could be measured by calorimeter or calculated by [30]

\[ Q_{(iso)} = \frac{-RT}{\ln q_e} \int \frac{d\ln c}{d(1/T)} \]  

(16)

where \( c \) is the retained concentration when the adsorption capacity is \( q \).

The integral form of Eq. (16) can be represented as

\[ Q_{(iso)} = 2.303RT_1T_2 \left( \frac{\ln c_{e1} - \ln c_{e2}}{T_1 - T_2} \right) \]  

(17)

<table>
<thead>
<tr>
<th>Table 3</th>
<th>Adsorption equilibrium constants obtained from Temkin and Dubinin-Radushkevich isotherms in adsorption of Cr(VI) on SAAEF</th>
</tr>
</thead>
<tbody>
<tr>
<td>( T/K )</td>
<td>( k/10^{-3} )</td>
</tr>
<tr>
<td>293</td>
<td>165.2</td>
</tr>
<tr>
<td>303</td>
<td>262.9</td>
</tr>
<tr>
<td>313</td>
<td>585.6</td>
</tr>
<tr>
<td>323</td>
<td>488.1</td>
</tr>
</tbody>
</table>
where \( T_1 \) and \( T_2 \) are 293 and 313 K, respectively; \( c_{e1} \) and \( c_{e2} \) are the equilibrium concentrations at \( T_1 \) and \( T_2 \), respectively.

The values of \( Q_{(iso)} \) at different adsorption capacities of Cr(VI) on SAAEF calculated by Eq. (17) are included in Table 4. \( Q_{(iso)} \) gets an increase with \( q_e \) increasing, which indicates an increase of the coverage ratio of SAAEF surface, and the energy distribution is not homogeneous on the SAAEF. Usually, the value of \( Q_{(iso)} \) is more than 42 kJ/mol when a chemisorption takes place while the value is in the range of 0.1−10 kJ/mol in a physisorption process. The value of \( Q_{(iso)} \) from 19.11 to 21.41 kJ/(mol·K) which is between the limited \( Q_{(iso)} \) values of the two kinds sorption proves that the adsorption of Cr(VI) on SAAEF involved both chemisorption and physisorption.

\( Q_{(iso)} \) gets an increase with \( q_e \) increasing, which is against the Freundlich and Temkin Models following the fact that \( Q_{(iso)} \) decreases with increasing \( q_e \). This explains the bad fitting of the Freundlich and Temkin models using the isotherm data.

### 3.6.2 Enthalpy change \( \Delta H \)

\( \Delta H \) can be obtained by the Clausius-Clapeyron equation represented as [30]

\[
\ln c = \frac{\Delta H}{RT} + k
\]

(18)

where \( c \) is the equilibrium concentration; \( T \) is the thermodynamic temperature; \( R \) is the mole gas constant (8.314 J/(mol·K)); \( k \) is a constant. From the isotherms at various temperatures, the adsorption isosteres of \( \ln c_e \) versus \( \frac{1}{RT} \) at different \( q_e \) values are displayed in Fig. 9. The values of \( \Delta H \) were obtained from the slope of the curve.

The negative value of \( \Delta H \) indicates the exothermic nature of the adsorption. The absolute value of \( \Delta H \) increases with the increase in temperature, which is in accordance with the change of \( Q_{(iso)} \) with temperature alteration.

### 3.6.3 Gibbs free energy change \( \Delta G \)

\( \Delta G \) is usually obtained by the Gibbs equation [30]:

\[
\Delta G = -RT \int_{0}^{x} \frac{dx}{q} \frac{\Delta H}{x}
\]

(19)

Fig. 9 Plot for \( \ln c_e \) versus \( 10^3(\frac{RT}{J·mol^{-1}})^{-1} \)

where \( x \) is the molar fraction of absorbate; \( q \) is the adsorption capacity.

The conversion formula between \( c \) and \( x \) for Cr(VI) can be expressed as

\[
c = 3.2 \times 10^6 x
\]

(20)

By putting Eqs. (5) and (20) to (19), the integral relation between \( c \) and \( \Delta G \) can be obtained and the values of \( \Delta G \) are given in Table 4.

The negative and decreased values of \( \Delta G \) with the increase in temperature reflect that the adsorption of Cr(VI) on SAAEF was a spontaneous process and spontaneity increased with the increase in temperature.

### 3.6.4 Entropy change \( \Delta S \)

\( \Delta S \) can be calculated by Gibbs-Helmholtz equation [31]:

\[
\Delta S = \frac{(\Delta H - \Delta G)}{T}
\]

(21)

where \( \Delta H \) is the enthalpy change; \( \Delta G \) is the Gibbs free energy change. The values of \( \Delta S \) are shown in Table 4.

The values of \( \Delta S \) are positive, indicating an increase in the randomness at the solid/liquid interface. Besides, the values of \( \Delta S \) increase with increasing temperature, suggesting that the degree of randomness increase getting larger [32].

<table>
<thead>
<tr>
<th>( q_e ) (mg/g)</th>
<th>( Q_{(iso)} ) (kJ·mol(^{-1}))</th>
<th>( \Delta H ) (kJ·mol(^{-1}))</th>
<th>( \Delta G ) (kJ·mol(^{-1}))</th>
<th>( \Delta S ) (J·mol(^{-1})·K(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td>( 293 ) K</td>
<td>( 303 ) K</td>
</tr>
<tr>
<td>90</td>
<td>19.11</td>
<td>−16.54</td>
<td>−15.47</td>
<td>−15.67</td>
</tr>
<tr>
<td>100</td>
<td>19.67</td>
<td>−16.70</td>
<td>−15.47</td>
<td>−15.67</td>
</tr>
<tr>
<td>120</td>
<td>21.41</td>
<td>−17.21</td>
<td>−15.47</td>
<td>−15.67</td>
</tr>
</tbody>
</table>

Table 4 Thermodynamic parameters for adsorption of Cr(VI) on SAAEF
4 Conclusions

1) SAAEF was found effective in the removal of Cr(VI) from aqueous solution and the maximum adsorption capacity reached 187.7 mg/g under optimal conditions.

2) FT-IR spectra suggest that the main functional groups on SAAEF did not change after the adsorption and the ion exchange took place on the surface of SAAEF.

3) The maximum adsorption capacity of Cr(VI) could be obtained at pH=1.0 and it increased with Cr(VI) concentration. The effect of temperature on the adsorption is unobvious.

4) The Langmuir, Freundlich, Dubinin-Radushkevich, Temkin models were adopted to describe the adsorption equilibrium isotherm data, respectively. Among all these models, the Langmuir and the Dubinin-Radushkevich models are in good agreement with the experimental data with high $R^2$ and reasonable calculated parameters.

5) The values of all the isotherm model constants indicate a favorable adsorption of Cr(VI) on SAAEF and an adsorption process involved both chemisorption and physisorption.

6) The values of thermodynamic parameters were calculated. The energy distribution on SAAEF is inhomogeneous because $Q_{(iso)}$ is not a constant value. The negative values of $\Delta H$, $\Delta G$ and positive $\Delta S$ suggest that the adsorption of Cr(VI) on SAAEF is a spontaneous, entropy-driven and endothermic process.

Acknowledgement

Many experiments were carried out by the assistance of WANG Yong.

References


摘 要：通过静态吸附实验，采用强碱性离子交换纤维(SAAEF)去除水溶液中的 Cr(VI)。分别研究了时间、Cr(VI)的初始浓度和 pH 对该吸附过程的影响。SAAEF 的最大饱和吸附量为 187.7 mg/g(pH=1)。饱和吸附量随着 Cr(VI)浓度的升高而增大，在 pH>1 的酸度范围内，随着 pH 值的增高而减少。采用 Langmuir、Freundlich、Dubinin-Radushkevich 和 Temkin 4 种热力学模型对不同温度的等温吸附曲线进行拟合，结果表明，Langmuir 等温吸附模型是描述 SAAEF 吸附 Cr(VI)热力学过程的最佳模型；模型参数表明，SAAEF 吸附 Cr(VI)的过程既存在物理吸附又存在化学吸附。热力学参数 ΔH、ΔG 和 ΔS 表明，该吸附过程为一放热、熵增的自发过程。热力学参数 Q(µ)不为常量，表明 SAAEF 表面存在能量分布不均匀的现象。

关键词：强碱性离子交换纤维；等温吸附线；热力学；化学吸附；物理吸附

(Edited by YANG Hua)