Experiment and simulation of diffusion of micron-particle in porous ceramic vessel

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Abstract: The general behavior of micron-particles in the inner domain of porous ceramic vessel was simulated by computational fluid dynamics software in terms of sampling experimental data. The results show that there is an optimum porosity of 0.32 to get a higher efficiency and lower pressure drop during filtration. According to the results of simulation and experiment, it is evident that lower inlet velocity can maintain lower pressure drop and obtain higher collection efficiency and inlet concentration also has a crucial influence on the collection efficiency. The collection efficiency of equipment increases significantly with the increase of inlet concentration when the inlet concentration is less than 6.3 g/m³, but it gradually tends to be stable in the range of 97.3%–99.7% when the inlet concentration is over this concentration.

Key words: micron particle; ceramic vessel; pressure drop; porous medium

1 Introduction

Micron-particles of flue gas generated by industrial coal-fired boilers and kilns can do great damage to ecological environment and public health. Due to the complex behavior of micron-particles in different flow media, especially porous medium, many investigators[1–2] have pursued the turbulent and diffusion mechanisms and numerical simulations to explore non-steady thermal and mass-transfer problems of contaminant particles with microscopic motions. CHENG et al[3] discussed the measurement method of ultrafine particle concentration and size distribution in an iron foundry. SUN et al[4] observed fine particle aggregating behavior induced by high intensity condition. YANG et al[5] analyzed the damage of fine particles reinforced metal matrix composite by ultrasonic method.


As an important dry-type dust-collecting device, its inner flow state directly affects many properties such as pressure drop, mass transfer in porous medium, convection and diffusion, and collection efficiency. Recently, some theoretical and numerical researches on the multiphase flow states in porous medium dust collecting device have been executed. SCHMIDT[10] investigated the influence of the interfacial drag on the pressure loss of combined liquid and vapor flow through particulate porous media. KUKRETI and...

On the basis of previous researches, this study mainly focuses on the procedure of mass transfer, convection and diffusion of nanoparticle aerosol through porous ceramic medium by using discrete particle model (DPM) and computational fluid dynamics (CFD) theory. Simultaneously, the corresponding characterization of carbon black and porous ceramic medium are presented. Finally, the experimental data are compared with the simulation results.

2 Theory and modeling

The incompressible Navier-Stokes (N-S) equations supplemented by computational fluid dynamics technology, some suitable turbulence models such as k—ε (Stand, RNG and Realizable) and Reynolds stress model (RSM) have provided theoretical basis for modeling the flow in porous ceramic vessel. The physical model consisting of inlet tube turbulence zone, dust hopper turbulence zone, porous laminar zone, clean gas turbulence zone and outlet tube turbulence zone is simulated by Euler-Lagrange discrete phase model because volume fraction of ultrafine particles is less than 10%. Moreover, the continuous phase in turbulence zone strictly satisfies N-S equation and discrete phase can use suitable discrete model.

2.1 Laminar flow

Since the velocity of mixture flow is very slow and the force is very small, the mixture flow (continuous phase and discrete phase) in porous laminar zone can be regarded as steady state Laminar flow. Considering the effect of friction of ceramic pores, the N-S equation should be revised to present the process of the discrete phase flowing through porous ceramic medium. The discrete and continuous flow can be respectively calculated according to the movement equations of discrete phase and the momentum equation of phase continuous. The model can be simulated by using CFD method according to the fixed bed adsorption theory proposed by AUGIER et al[13] and the solving method of flow behavior and particle dispersivity of granular flow reported by JAFARI et al[14]:

$$\frac{\partial u_i}{\partial x_i} = 0$$  \hspace{1cm} (1)

for continuity of continuous phase and

$$\frac{\partial (\phi \rho u_i)}{\partial t} + \text{div}(\phi \rho u u_i) = \phi_i \cdot \text{grad}(u_i) + \phi_i F$$  \hspace{1cm} (2)

for momentum.

where $u_i$ is the fluid velocity in porous zone, $\phi$ is porosity, $\rho$ is fluid density, $x_i$ is flow distance in direction $i$, $u$ is velocity, $t$ is time, $\mu$ is fluid dynamic viscosity and $F$ is source item.

There are three assumptions in porous zone: a uniform velocity is assumed in the porous zone, no transition zone is generated at the gas-solid interfaces and no transversal slip occurs in pathlines direction.

2.2 Turbulent flow

Due to the mass conservation for all flows, the mass increment in a unit volume per unit time equals to the mass difference between the inlet and outlet of the unit volume. So, the continuity equation is

$$\frac{\partial \rho}{\partial t} + \frac{\partial}{\partial x_i} (\rho u_i) = 0$$  \hspace{1cm} (3)

Eq.(3) is the general form of the mass conservation equation and is valid for incompressible flow. Due to no special phenomenon in turbulent flow such as phase transformation, the source is defined as zero.

Since all flow cases must satisfy momentum conservation law, that is, the Newton’s second law, so the momentum transfer equation of system is

$$\frac{\partial}{\partial t} (\rho u_i) + \frac{\partial}{\partial x_j} (\rho u_i u_j) = -\frac{\partial p}{\partial x_i} + \frac{\partial}{\partial x_j} \left( \mu \left( \frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right) \right) + F_i$$  \hspace{1cm} (4)

where $i, j$ represent two different directions, $p$ is pressure on a fluid micro element, $F_i$ is the momentum source that includes two parts resulted by porous zone: the former is viscous resistance loss caused by Darcy’s percolation process and the latter is inertial resistance loss caused by the permeability of porous media. The formula of $F_i$ is

$$F_i = \frac{\mu}{\alpha} u_i + C_2 \frac{1}{2} \rho \left| u_i \right| u_j$$  \hspace{1cm} (5)

where $1/\alpha$ is viscous resistance coefficient and $C_2$ is inertial resistance coefficient. To simply computation of coefficient $1/\alpha$ and $C_2$, the porous ceramic media are regarded as homogenous.

The standard type of $k—\varepsilon$ equation is based on the hypothesis of isotropic eddy-viscosity, which is modeled through the flow fields of the turbulent kinetic energy and the specific dissipation rate[15]. Considering the effect of turbulent swirl, low-Reynolds-number and near-wall region, the RNG $k—\varepsilon$ model was derived using a rigorous statistical technique to enhance accuracy for swirling flows. In this work, RNG $k—\varepsilon$ model is applied...
in all non-porous flow zones. The transport equations of RNG \( k-\varepsilon \) model are

\[
\frac{\partial}{\partial t}(\rho k) + \frac{\partial}{\partial x_i}(\rho k u_i) = \frac{\partial}{\partial x_j}\left(\alpha_k \mu_{eff} \frac{\partial k}{\partial x_j}\right) +
\]

\[
- \mu_t \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - \rho \varepsilon + C_{1\varepsilon} \frac{\mu}{k} \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - \frac{\varepsilon}{k} R_c \tag{6}
\]

\[
\frac{\partial}{\partial t}(\rho \varepsilon) + \frac{\partial}{\partial x_i}(\rho \varepsilon u_i) = \frac{\partial}{\partial x_j}\left(\alpha_\varepsilon \mu_{eff} \frac{\partial \varepsilon}{\partial x_j}\right) +
\]

\[
\frac{C_{\mu\varepsilon}}{k} \mu_t \left( \frac{\partial u_j}{\partial x_i} + \frac{\partial u_i}{\partial x_j} \right) - C_{2\varepsilon} \rho \frac{\varepsilon^2}{k} - R_c \tag{7}
\]

where \( k \) is turbulent kinetic energy; \( \varepsilon \) is dissipation rate; \( \mu_{eff} \) is effective viscosity; \( \mu_t \) is turbulent viscosity; \( C_{1\varepsilon} \) and \( C_{2\varepsilon} \) are constants; \( \alpha_k \) and \( \alpha_\varepsilon \) are respectively the inverse effective Prandtl numbers for \( k \) and \( \varepsilon \); \( \eta = S_\varepsilon/\varepsilon; \eta_0 = 4.38 \); \( \beta = 0.012 \); \( C_\mu = 0.0845 \); \( S_k \) is user-defined source term.

In Eq.(7), the additional term \( R_c \) makes model more responsive to the effects of rapid strain and streamline curvature than the standard \( k-\varepsilon \) model.

2.3 Discrete phase

The surface morphologies of carbon black particles were investigated by JSM-6700F field emission scanning electron microscope (FE-SEM). The typical crystallite of carbon black nanoparticles is shown in Fig.1. It is evident that the general carbon black particles appear as spherical crystallite micro-particles with the size of about 100 nm in standard state. The crystalline phases of supported samples in the fly-ash state were studied by X-ray diffractometry (XRD) (Fig.2). The chemical composition of compound phases was estimated according to the lattice parameter offset calculated by the angular position of the metal reflections using the Vegard’s law. Identification result of carbon black sample shows that the chemical composition is mainly composed of \( \text{PbF}_2, \text{SiO}_2, \text{C}_60, \text{CaCO}_3 \) and \( \text{Al}_2\text{O}_3 \). This result matches with microanalysis report of EDX test properly.

In this work, we presumed that carbon black particles rebound back or deposit on the filter after colliding with the wall. The deposit processes satisfy particle erosion and accretion theory. According to statistical cumulative undersize distribution using 400 particle samples of 8 FE-SEM photographs, it shows that the carbon black nanoparticles obey Rosin-Rammer (R-R) distribution. The cumulative undersize distribution is

\[
\lg \left[ \ln \left[ \frac{1}{(1-G)} \right] \right] = n \lg \left( \frac{d_p}{\bar{d}_p} \right) + n \lg d_p \tag{9}
\]

where \( d_p \) is the measured carbon black equivalent diameter; \( n \) is the distribution exponent; \( \bar{d}_p \) is carbon black equivalent mean diameter when \( G=0.632 \). The corresponding parameters in R-R distribution are obtained by experiment and interpolation: \( n=0.8263 \); \( \bar{d}_p = 34.254 \) nm, the minimum equivalent diameter is 9.05 nm and the maximum equivalent diameter is 190.68 nm. The fitting curve of R-R distribution matches with experimental data properly, as shown in Fig.3.
In the model, particles injection and air flow inlet lie on the same inlet surface. The discrete phase composed of carbon black nanoparticles has the specific motion equation. Due to the interaction between air and sub-micron particles in actual movements, the turbulent movement of air will improve or impede the motion of discrete phase in non-porous zones. Particle drag force from mixing and coupling process between continuous phase and discrete phase produces coupling movement velocity to interact each other. The motion equation of a spherical aerosol particle with consideration of the nonlinear drag force, Saffman Lift Force and the gravitational force is given as\[16\]

\[
\frac{du_p}{dt} = F_d + F_L + B_r + G
\]

where \(u_p\) is the carbon black nanoparticles velocity; \(F_d\) is the drag force; \(F_L\) is the Saffman lift force; \(B_r\) is Brownian random and \(G\) is the gravity.

### 2.4 Physical characteristics of porous ceramic vessel

General speaking, there are several kinds of pore diameter series in adsorbent and the equivalent radius of every series has a certain range. According to the definition presented by Dubinin et al[17], the pore diameter can be divided into four ranges: the pore channel is defined as micropore \((r_p<0.6−0.7\text{ nm})\), sub-mesopore \((0.6−0.7\text{ nm} < r_p < 1.5−1.6\text{ nm})\), mesopore \((1.5−1.6\text{ nm} < r_p < 100−200\text{ nm})\) and macropore \((r_p > 100−200\text{ nm})\). The diffusion mechanism of particle pollutant is correlative with pore diameter, adsorbate concentration, pressure drive, temperature difference, etc. The diffusion in the porous media can be described by Fick’s Law[18].

The surface morphologies and chemical composition were tested by TEM−3010 high resolution transmission electronic microscope. The typical crystallite of ceramic material is shown in Fig.4. It is evident that the general ceramic particle appears to rough edge ellipsoidal crystallite particle with the size of about 1 μm in standard state. Huang et al[19] developed an approach of quantitative measurement of porosity and pore size distribution, which is employed in the present study. By this way, we can take the logarithm of equivalent pore diameters and divide them into 20 levels. With 80 fields in a single measure and 10 times of repeated measure, we could obtain the average value in the porous media with different porosities respectively. Identification result of ceramic material sample shows that the chemical composition is mainly composed of \(\text{Ca}_2\text{SiO}_4\), \((\text{KPO}_3)_4\cdot12\text{H}_2\text{O}\), mullite, \(\text{CoCl}_2\cdot6\text{H}_2\text{O}\), \(\text{W}_2\text{N}\) (Fig.5).

This model forms a closed domain by many porous ceramic media vessels and the basic work principle is similar to that of bag filter. Actually there are obvious differences from bag filter in the filtration mechanism. The work principle of bag filter is that the powder dusts are accumulated into prime layer on the bag surface by particles interception, inertia collision, electrostatic force and diffusion. Particularly the prime layer of bag filter becomes the main filtration layer[20]. Besides the efficacy of bag filter, many complex physical and chemical phenomena of ultrafine particle occur such as mass transfer, convection, diffusion and adsorption in the inner porous zones of porous ceramic media tubes. In this work, the physical transfer of aerosol contamination is mainly considered in the coupling process of carbon black and porous media by ignoring the influence of chemical reaction, which includes diffusion and adsorption. Mass diffusion coefficients are used to compute the diffusion flux of a chemical species in a laminar flow using Fick’s Law[21]:

\[
J_i = -\rho_c D V C_i
\]

where \(J_i\) is the diffusion flux of contaminant; \(\rho_c\) is the density of contaminant; \(D\) is the dynamic dispersivity.

![Fig.4 TEM photograph for porous ceramic media absorbent](image1)

![Fig.5 XRD patterns of porous ceramic media](image2)
where $D^*$ is the sum of sub-micron particles dispersivity coefficient and mechanical dispersivity coefficient.

$$D = D_d + D^*$$  \hspace{1cm} (13)

where $D_d$ is sub-micron particles dispersivity coefficient, $D^*$ is mechanical dispersivity coefficient.

Dispersivity coefficient of sub-micron particles depends on contamination permeation velocity $u$ in porous media, Pelet number and geometric characteristics of porous media.

$$D^* = \frac{ud}{Pe}$$  \hspace{1cm} (14)

where $u$ is the permeation velocity; $d$ is the mean diameter of ceramic granular; $Pe$ is the Pelet number.

The test results of metallographic microscope show that porous ceramic media property is stable and the pore size distribution of porous media satisfies Gaussian distribution. Consequently, the hypothesis of isotropy of porous media satisfies Gaussian distribution.

Additionally, the mass transfer process satisfies linear drive force (LDF) equation[13, 23]:

$$\frac{\partial \phi}{\partial t} = K(q_i^* - q_i)$$  \hspace{1cm} (16)

where $q$ is the mass of contaminant deposited on porous media; $q_i^*$ is the deposit mass of contaminant at equilibrium; $q_i$ is the instantaneous deposit mass.

### 2.5 User define functions (UDFs)

As an essential supplementary of variable LDF and variable concentration of discrete phase, user define functions (UDFs) are important custom-defined forms of variable scalar because there is no variable drag force source provided for the coupling process of discrete phase and porous media zone and the contamination transfer-dispersivity-adsorption equation is not contained in the standard form of Fluent software. In this work, some coupled mixtures of carbon black nanoparticles and continuous phase flow into the macropore firstly; and the remains flow into mesopore and sub-mesopore after parts of them are absorbed by macropore, and then a small amount of mixture flows into micropore after parts of them are intercepted by mesopore and sub-mesopore; finally, the trace gaseous contaminants permeate into intra-particle zone after parts of them are absorbed and intercepted by micropore. The contamination adsorbates present parabolic distribution in the inner zone of adsorbent.

The above process can be simplified by Gluckauf’s linear driving force model (LDFM) in UDFs, that is, the computation process is simplified greatly when LDFM is used as partial differential equation drive force model for material balance to make contamination particles diffuse onto adsorbent surface from continuous phase driven by concentration difference drive force $\Delta q$.

Function Define_Dpm_Source is used to define the source item of discrete phase equation, the general expression of which is

$$S_{\varphi} = S_c + S_{\delta} \phi$$  \hspace{1cm} (17)

where $\phi$ is dependent variable; $S_c$ is the explicit part of the source term; $S_{\delta} \phi$ is the implicit part of the source term.

### 3 Results and discussion

#### 3.1 Resistance characteristic of porous media

Fig.6 presents the relationship of system pressure drop and inlet velocity under different porosities. It is evident that the finer porosity in the calculation domain has more significant effect on the variation of curves while the effect of larger porosity is very weak. In this simulation, it is found that the porous media with $\varphi=0.35$ have the weakest effect and the porous media with $\varphi=0.30$ have the most effect under the operating conditions...
conditions. At the inlet velocity of 4 m/s, the pressure loss decreases by 250 Pa while the porosity varies from 0.30 to 0.35. At the inlet velocity of 8 m/s, the pressure loss decreases by 600 Pa while the porosity varies from 0.30 to 0.35. If keeping the porosity as a constant, the $P - V$ presents parabolic curve regularly. Since the flow state belongs to low velocity range ($u \leq 10$ m/s), however, the tendency curve approaches linear law approximately. Fig.7 shows the comparison of tendency curve of pressure drop and collection efficiency with porosity. The perfect condition for dust-collecting device is low resistance and efficient dust-collecting performance in practical application. In fact, the two cases are contradictory: if the efficient dust-collecting performance is obtained, then the pressure drop is large and vice versa. So, we must seek an optimum porosity of pressure drop and collection efficiency for system. According to the two curves in Fig.7, it is found that the collection efficiency ($\eta$) can attach 99.3% and pressure drop of system is lower than 1 000 Pa when the porosity is 0.32, which exactly meets the requirements of practical operation. The pressure loss increases by 720 Pa with the porous media at the porosity of 0.32 when the inlet velocity varies from 4 to 9 m/s, as reported in Fig.8. Compared the experimental data with RNG $k-\varepsilon$ simulation curve, the clustering tendency of data point near the simulation curve is observed distinctly, which shows that the RNG $k-\varepsilon$ simulation results accord with the actual work.

System pressure loss mostly comes from viscosity resistance and inertial resistance of porous media, friction pressure loss and local pressure loss of pipe. Resistance coefficients of various porous media are listed in Table 1 in terms of experimental ceramic vessels and derivation of Ergun’s equation. It is verified by simulation and experiment that pipe pressure loss is far less than resistance of porous media, that is, pipe pressure loss can be ignored comparatively. Thereby, system pressure loss is favorably induced as the theoretical parabolic curve formulation of porous media.

$$\Delta p = au^2 + bu$$  \hspace{1cm} (18)$$

where $au^2$ is the corresponding item of Darcy’s permeating pressure loss, and $bu$ is the corresponding item of inertial resistance.

![Fig.6](image1)  \hspace{1cm} **Fig.6** Relationship between pressure drop $\Delta p$ and inlet velocity $u$ corresponding to different porosities

![Fig.7](image2)  \hspace{1cm} **Fig.7** Relationship of $\eta$ and $\phi$ with $\phi$ at inlet velocity of 7.325 m/s and inlet concentration of 4.5 g/m³

![Fig.8](image3)  \hspace{1cm} **Fig.8** Comparison of experimental data and simulation curve of $\Delta p-\mu$ with porosity of 0.32

| Table 1 | Resistance coefficients of various porous media |
| --- | --- | --- |
| $\phi$ | $\alpha^{-1}$/m² | $C_s$/m⁻¹ |
| 0.301 | 2.30×10¹¹ | 8.30×10⁵ |
| 0.305 | 2.20×10¹¹ | 7.95×10⁵ |
| 0.31 | 2.06×10¹¹ | 7.52×10⁵ |
| 0.35 | 1.27×10¹¹ | 4.92×10⁵ |
3.2 Frequency distribution of escaping dust particles

The experiments are performed for the porous media with porosity of 0.32 and mean pore diameter of 5.12 μm and the dust samples have maximum equivalent of 190.68 nm and mean equivalent of 34.254 nm. Since the pore diameter of porous media is far larger than the free path of particles, the dust particles act as bulk diffusion inside the capillary tubes of porous media[24]. The main movements are inter-particles collisions and the accidents of particles-to-wall collisions belong to little probability. As a consequence, the corresponding modification for diffusion coefficient only need consider porosity $\phi$ and tortuosity factor $\tau$. Then the modified diffusion coefficient is

$$D_D = \frac{D_e}{\tau}$$ (19)

The removing principle of dust contamination using porous ceramic mainly depends on the collision and adhesion with complex tortuosity capillary channels and tubes. Since the particle size of 9.05–197.32 nm is far less than the pore size, the probabilities of capturing the carbonblack particles with any size are nearly equal. So, the frequency distribution of escaping particles basically remains 8–12% (Fig.9).

3.3 Collection efficiency

Fig.10 illustrates the comparison of the collection efficiencies of simulations and experiments at three experimental velocities: 6.24 m/s, 7.33 m/s and 7.84 m/s. The result shows that the collection efficiency of simulation is coincident with the experimental data and it enhances with increasing the inlet concentration of aerosol contaminant. As shown in Fig.10, the experimental collection efficiency can reach 96.7%–98.02% and the theoretical collection efficiency computed by CFD can reach 97.3%–99.7% at $C_{in} \geq 6.3$ g/m$^3$ and it enhances obviously with decreasing the flow velocity.

![Fig.9 Frequency distribution histogram of escaping particles on outlet surface](image)

![Fig.10 Collection efficiency comparison of simulations and experiments in three schemes](image)

4 Conclusions

1) A numerical model of porous ceramic medium filter is implemented by experiment and CFD simulation in this study. It is found that the current porosity during the filtration of carbon black nanoparticles has enormous influence on the pressure drop and collection efficiency. The result shows that if the porosity is too small, the collection efficiency is high but the pressure loss will severely rises, and vice versa. This study indicates that the porosity of $\phi=0.32$ is the optimum intersection point of pressure drop and collection efficiency.

2) The study proves that the method of separation and filtration of carbon black nanoparticles from flue flow is feasible by porous ceramic media with the porosity of micron size. From the analysis of escaping particles distribution and collection efficiency, the sensitivity of carbon black nanoparticles to pore diameter size is weak and to porosity $\phi$ or tortuosity factor $\tau$ is high.

3) The medium and low inlet gas velocity can get higher collection efficiency. In the low concentration range, collection efficiency increases quickly with the concentration rising. The efficiency curves gradually tend to be steady in the high concentration range.

References


