

# MODEL OF CONDUCTIVITY IN DOPED $\text{SnO}_2$ -BASE INERT ANODES FOR AL-ELECTROWINNING<sup>①</sup>

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## ABSTRACT

The variations of chemical bonding characteristics in doped  $\text{SnO}_2$ -base inert anodes with various dopants are studied using CNDO/2 quantum chemical calculations. A new model of conductivity is derived, which is checked with literature data and our experimental results. Proper dopants can be selected with the model to reduce the resistivity of said electrode effectively.

**Key words:** doped  $\text{SnO}_2$ -base inert anodes quantum chemistry conductivity dopants

## 1 INTRODUCTION

Since the  $\text{SnO}_2$ -base inert anode was applied to the electrowinning process of aluminum from the cryolite- $\text{Al}_2\text{O}_3$  molten salts in 1930s, much work has been done about the conductivity of the anode and how to raise it by doping. Xue *et al.*<sup>[1]</sup> adopted the 2-probe method to detect the resistivity of the anode and found that its conductivity can be raised by controlling the valence of the dopant or promoting the sintering process of the anode when it is doped by  $\text{Sb}_2\text{O}_3$ ,  $\text{CuO}$  or  $\text{ZnO}$ . Wang *et al.*<sup>[2]</sup> studied the effect of the six dopants of  $\text{Sb}_2\text{O}_3$ ,  $\text{CuO}$ ,  $\text{ZnO}$ ,  $\text{MnO}_2$ ,  $\text{Fe}_2\text{O}_3$  and  $\text{Cr}_2\text{O}_3$  on the physical properties of the anode such as the resistivity with plural progressive regression. In this paper, the variations of the chemical bonding characteristics in doped  $\text{SnO}_2$ -base inert anodes are studied with

CNDO/2 quantum chemical calculations. By investigating the mechanism of the conduction of electricity in the doped anodes, a new model of conductivity is derived, which is checked with literature data and our experimental results. Proper dopants can be selected with the model to reduce effectively the resistivity of the anodes.

## 2 QUANTUM CHEMICAL CALCULATIONS

### 2.1 Calculation Method

CNDO/2 calculations are adopted which are well applicable for the comparison of the electric or magnetic properties in homologues. The program is run on a Siemens 7570C computer with the necessary atomic parameters from Pople *et al.*<sup>[3]</sup>.

A  $\text{SnO}_2$  unit cell with 15 atoms and 24

net charges shown in Fig.1 is taken as the calculation model of the  $\text{SnO}_2$ -base. All the atoms in the model are numbered from 1 to 15. In order to examine the effect of every dopant on the bonding characteristics of the  $\text{SnO}_2$  unit cell,  $\text{Sn}^{4+}$  is replaced by a metallic cation of the dopant. As is known<sup>[4]</sup>, many metallic cations are almost the same in radii as  $\text{Sn}^{4+}$  and often take the place of  $\text{Sn}^{4+}$  in natural tinstone in isomorphous form. Therefore, we can choose such cations as  $\text{Sb}^{3+}$ ,  $\text{Cu}^{2+}$ ,  $\text{Zn}^{2+}$ ,  $\text{Mn}^{4+}$ ,  $\text{Cr}^{3+}$ ,  $\text{Ni}^{2+}$ ,  $\text{Ti}^{4+}$ ,  $\text{V}^{5+}$ ,  $\text{Co}^{3+}$ ,  $\text{Y}^{3+}$ ,  $\text{Zr}^{4+}$ ,  $\text{Nb}^{5+}$ ,  $\text{Bi}^{5+}$  and  $\text{Ir}^{4+}$ , the radii of which are almost the same as that of  $\text{Sn}^{4+}$ <sup>[5]</sup>, to replace  $\text{Sn}^{4+}$  in our calculations. The corresponding dopants of oxide are  $\text{Sb}_2\text{O}_3$ ,  $\text{CuO}$ ,  $\text{ZnO}$ ,  $\text{MnO}_2$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{Cr}_2\text{O}_3$ ,  $\text{NiO}$ ,  $\text{TiO}_2$ ,  $\text{V}_2\text{O}_5$ ,  $\text{Co}_2\text{O}_3$ ,  $\text{Y}_2\text{O}_3$ ,  $\text{ZrO}_2$ ,  $\text{Nb}_2\text{O}_5$ ,  $\text{Bi}_2\text{O}_3$  and  $\text{IrO}_2$ . The  $\text{Sn}^{4+}$  to be replaced is selected from the centre of the unit cell so that the calculation results are symmetrical. It is supposed that the lattice parameters of the  $\text{SnO}_2$  unit cell remain constant after the replacement of  $\text{Sn}^{4+}$  by the cations. The necessary lattice parameters of  $\text{SnO}_2$  for counting the

coordinated of every atom are taken from Samsonov<sup>[6]</sup>.

## 2.2 Calculation Results

The compositions of the highest occupied molecular orbitals (HOMO) of  $\text{SnO}_2$  and doped  $\text{SnO}_2$  unit cells are obtained with CNDO / 2 calculations. The atoms are classified as shown in Table 1, where the numbers refer to those of the numbered atoms and where oxides (except  $\text{SnO}_2$ ) refer to the dopants in  $\text{SnO}_2$  unit cell. The atoms that participate in the formation of HOMO are marked as  $\checkmark$ .

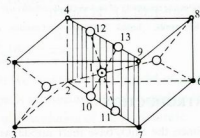


Fig. 1 The whole unit cell of  $\text{SnO}_2$

●— $\text{Sn}^{4+}$  ○— $\text{O}^{2-}$  ⊙— $\text{Sn}^{4+}$  or doped ion

Table 1 Atoms participating in HOMO formation of  $\text{SnO}_2$  and  $\text{SnO}_2$  unit cells

	$\text{SnO}_2$	$\text{Sb}_2\text{O}_3$	$\text{CuO}$	$\text{ZnO}$	$\text{MnO}_2$	$\text{Fe}_2\text{O}_3$	$\text{Cr}_2\text{O}_3$	$\text{NiO}$	$\text{TiO}_2$	$\text{V}_2\text{O}_5$	$\text{Co}_2\text{O}_3$	$\text{Y}_2\text{O}_3$	$\text{ZrO}_2$	$\text{Nb}_2\text{O}_5$	$\text{Bi}_2\text{O}_3$	$\text{IrO}_2$
1	✓		✓		✓	✓	✓	✓	✓	✓		✓	✓	✓	✓	✓
2		✓		✓	✓	✓	✓		✓	✓		✓	✓	✓		
3			✓			✓	✓			✓	✓		✓	✓		
4		✓			✓	✓	✓		✓	✓		✓	✓	✓		
5			✓			✓	✓			✓	✓		✓	✓		
6			✓			✓	✓			✓	✓		✓	✓		
7		✓		✓	✓	✓	✓		✓	✓		✓	✓	✓		
8			✓			✓	✓			✓	✓		✓	✓		
9		✓		✓	✓	✓	✓			✓	✓		✓	✓		
10	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓			✓	✓	✓	
11	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓			✓	✓	✓	
12	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓			✓	✓	✓	
13	✓	✓	✓	✓	✓	✓	✓	✓	✓	✓			✓	✓	✓	
14	✓		✓			✓	✓	✓		✓	✓		✓	✓	✓	✓
15	✓		✓			✓	✓	✓		✓	✓		✓	✓	✓	✓

### 3 THE MODEL OF CONDUCTIVITY

$\text{SnO}_2$  and doped  $\text{SnO}_2$ -base anodes are semiconductors in which the simulated electrons in HOMO conduct electricity. Therefore only the atoms which participate in the formation of HOMO supply the electrons to form electricity. In  $\text{SnO}_2$  anode, the atoms which participate in the formation of HOMO and supply the electrons to form electricity are those numbered 1, 10, 11, 12, 13, 14, 15 and situated in all three dimensions. As a result, the resistance of the lattice to the flow of electrons to form electricity is large, i. e. the resistivity of the anode is large and its conductivity small.

When the  $\text{SnO}_2$ -base is doped by  $\text{Sb}_2\text{O}_3$ , the atoms which participate in the formation of HOMO and supply the electrons to form electricity change to those numbered 2, 4, 7, 9, 10, 11, 12, 13. They are located on one plane which is depicted by the shaded area in Fig. 1. The resistance of the lattice to the flow of the electrons on the plane to form electricity becomes smaller and thus the resistivity of this doped  $\text{SnO}_2$ -base anode is reduced and its conductivity raised. Such dopants as  $\text{ZnO}$ ,  $\text{MnO}_2$ ,  $\text{TiO}_2$ ,  $\text{Co}_2\text{O}_3$  and  $\text{IrO}_2$  have the same function as  $\text{Sb}_2\text{O}_3$ . Conductivity of the  $\text{SnO}_2$ -base anode with any of these dopants will be raised.

When the  $\text{SnO}_2$ -base is doped by  $\text{Fe}_2\text{O}_3$ , the atoms which supply the electrons to form electricity change to 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14 and 15. That is, all the atoms in the lattice participate in the formation of HOMO. They are situated in all three dimensions rather than on one plane. The resistance of the lattice to the flow of electrons to form electricity is increased. Therefore the addition

of  $\text{Fe}_2\text{O}_3$  to the  $\text{SnO}_2$ -base anode will reduce the conductivity of the anode. Such dopants as  $\text{CuO}$ ,  $\text{Cr}_2\text{O}_3$ ,  $\text{NiO}$ ,  $\text{V}_2\text{O}_5$ ,  $\text{Y}_2\text{O}_3$ ,  $\text{ZrO}_2$ ,  $\text{Nb}_2\text{O}_5$  and  $\text{Bi}_2\text{O}_3$  have the same function as  $\text{Fe}_2\text{O}_3$ . The atoms participating in the formation of HOMO in the  $\text{SnO}_2$ -base anode doped by any of above dopants are situated in all three dimensions.

Only one  $\text{Sn}^{4+}$  in the centre of the  $\text{SnO}_2$  unit cell is replaced by a cation of dopant in our CNDO / 2 calculations. Therefore the above-mentioned new model of conductivity is applicable only for the doped  $\text{SnO}_2$ -base anodes with the model at a too high or too low concentrations. In addition, as the results of quantum chemical calculations reveal, in theory, the bonding characteristics at the temperature of absolute zero, any difference in the conductivity of the anode caused by the variation of its physical or chemical properties with increasing temperature is neglected in the model.

### 4 VERIFICATION OF THE MODEL

From the new model of conductivity, it is known that atoms participating in the formation of HOMO are located on one plane if the  $\text{SnO}_2$ -base anode is doped by  $\text{Sb}_2\text{O}_3$ ,  $\text{ZnO}$ ,  $\text{TiO}_2$ ,  $\text{Co}_2\text{O}_3$  or  $\text{IrO}_2$ . The electrons in them are easily stimulated and flow on the plane to form electricity. The resistance of the lattice to the flow of the electrons to form electricity is decreased. So the resistivity of any of these doped  $\text{SnO}_2$ -base anode is reduced and its conductivity raised. If the  $\text{SnO}_2$ -base anode is doped by  $\text{Fe}_2\text{O}_3$ ,  $\text{CuO}$ ,  $\text{Cr}_2\text{O}_3$ ,  $\text{NiO}$ ,  $\text{V}_2\text{O}_5$ ,  $\text{Y}_2\text{O}_3$ ,  $\text{ZrO}_2$ ,  $\text{Nb}_2\text{O}_5$  or  $\text{Bi}_2\text{O}_3$ , atoms participating in the formation of HOMO are situated in all three dimensions. The resistance of the lattice to the flow of the electrons supplied by

these atoms to form electricity is increased. The resistivity of any of these doped  $\text{SnO}_2$ -base anodes is raised and its conductivity reduced. The above prediction of the variation of conductivity is checked with literature data and our experiments as follows.

#### 4.1 The Experimental Conditions

$\text{SnO}_2$  and doped  $\text{SnO}_2$ -base anodes were prepared by powder sintering<sup>[7]</sup>.  $\text{SnO}_2$  and all the dopants of oxide were reagent grade. The anodes were pressed and shaped before sintered at 1,350°C in air for 5 h. They were cylindrical with a length to diameter ratio greater than 3. All the anodes were prepared in one batch with the same technique to make sure that they were comparable. A four-probe method was adopted to measure the conductivities of the anodes in view of the stabilities of semiconductors<sup>[7]</sup>.

#### 4.2 The Experimental Results

$\text{SnO}_2$ -base anodes doped by  $\text{TiO}_2$ ,  $\text{V}_2\text{O}_5$ ,  $\text{Co}_2\text{O}_3$ ,  $\text{Y}_2\text{O}_3$ ,  $\text{Bi}_2\text{O}_5$  and  $\text{Nb}_2\text{O}_5$  were prepared. Their conductivities together with some of their physical properties were measured as shown in Table 2. All of them were the average values of more than 2 measurements. The amounts of the dopants in  $\text{SnO}_2$  were 1~3 wt-%.

Table 2 shows that the conductivity of the

$\text{SnO}_2$ -base anode doped by  $\text{TiO}_2$  or  $\text{Co}_2\text{O}_3$  is greatly raised while that of the  $\text{SnO}_2$ -base anode doped by  $\text{V}_2\text{O}_5$  or  $\text{Y}_2\text{O}_3$  is reduced, which coincides with the model. The conductivity of  $\text{Bi}_2\text{O}_5$  or  $\text{Nb}_2\text{O}_5$  doped  $\text{SnO}_2$ -base anode is slightly increased, which seems to contradict with the model. But as is known<sup>[8]</sup>,  $\text{Bi}_2\text{O}_5$  and  $\text{Nb}_2\text{O}_5$  easily lose their oxygen at high temperatures to become nonstoichiometric with their conductivities raised. By comparing the increase of the conductivities in a  $\text{Bi}_2\text{O}_5$  or  $\text{Nb}_2\text{O}_5$  doped and a  $\text{TiO}_2$  or  $\text{Co}_2\text{O}_3$  doped  $\text{SnO}_2$ -base anodes, we notice that the conductivity of a  $\text{Bi}_2\text{O}_5$  or  $\text{Nb}_2\text{O}_5$  doped  $\text{SnO}_2$ -base anode is not raised greatly even though there exist defects and the nonstoichiometry of oxygen in  $\text{Bi}_2\text{O}_5$  and  $\text{Nb}_2\text{O}_5$ .

The variations of conductivity in doped  $\text{SnO}_2$ -base anodes predicted from the new model are listed in Table 3 with the literature data and our experimental results. Table 3 indicates that the literature data and our experimental results coincide well with the predicted conductivities, which supports the model very well. In addition, the conductivity of the  $\text{SnO}_2$ -base anode doped by  $\text{CuO}$  is reduced at low temperatures. This is identical with the prediction of the model. But the physical and chemical properties of  $\text{CuO}$  vary at high temperatures because of the formation of the  $\text{CuO-Cu}_2\text{O}$  liquid phase which can wet the  $\text{SnO}_2$

Table 2 The conductivities of doped  $\text{SnO}_2$ -base inert anodes

No.	component	density / g.cm <sup>-3</sup>	porosity / %	conductivity / × 10 <sup>-4</sup> Ω <sup>-1</sup> cm <sup>-1</sup>				
				600 / °C	700 / °C	800 / °C	900 / °C	970 / °C
028SA01	$\text{SnO}_2$	4.083	41.77			0.509	3.401	13.24
038SA01	$\text{SnO}_2$ - $\text{TiO}_2$	4.252	39.10	16.6	127	590	1231	1536
036SA01	$\text{SnO}_2$ - $\text{V}_2\text{O}_5$	5.286	22.96			1.822	3.081	6.027
025SA01	$\text{SnO}_2$ - $\text{Co}_2\text{O}_3$	5.266	24.96	531	2451	4161	5958	7181
032SA01	$\text{SnO}_2$ - $\text{Y}_2\text{O}_3$	4.539	37.34			0.483	2.857	8.14
039SA01	$\text{SnO}_2$ - $\text{Bi}_2\text{O}_5$	6.822	0.052			6.812	20.07	37.49
030SA02	$\text{SnO}_2$ - $\text{Nb}_2\text{O}_5$	5.120	26.04		7.474	29.50	93.43	

crystalline grain to reduce greatly the porosity of the anode and enhance the contact between the crystalline grains to reduce the contact resistance. As a result of that, the sintering process is promoted and the conductivity of the anode is raised at high temperatures.

**Table 3** The predicted (p.) and experimental (e.) conductivities of doped SnO<sub>2</sub>-base inert anodes\*

dopant	Sb <sub>2</sub> O <sub>3</sub>	CuO	ZnO	MnO <sub>2</sub>	Fe <sub>2</sub> O <sub>3</sub>	Cr <sub>2</sub> O <sub>3</sub>	NiO	
p.	↑	↓	↑	↑	↓	↓	↓	
e.	↑ [1,2]	↓ [1,2]	↑ [1,2]	↑ [1]	↓ [1,2]	↓ [1]	↓ [2]	
	TiO <sub>2</sub>	V <sub>2</sub> O <sub>5</sub>	Co <sub>2</sub> O <sub>3</sub>	Y <sub>2</sub> O <sub>3</sub>	ZrO <sub>2</sub>	Nb <sub>2</sub> O <sub>5</sub>	Bi <sub>2</sub> O <sub>3</sub>	IrO <sub>2</sub>
	↑	↓	↑	↓	↓	↓	↓	↑
	[author]	[author]	[author]	[author]	[author]	[author]	[author]	[author]

\* — at low temperature; ↑ — raise; ↓ — reduction;

[ ] — references

The effect of the remaining of the dopants in Table 3 on the conductivities of the SnO<sub>2</sub>-base anodes needs to be checked further due to the lack of chemical reagents.

From the above discussion, it is known that the conductivity of any binary doped SnO<sub>2</sub>-base anode can be predicted correctly with CNDO/2 calculations of quantum chemistry and the new model of conductivity, which provides a convenient way to select proper dopants of oxide to raise the conductivity of the SnO<sub>2</sub>-base inert anode.

## 5 CONCLUSIONS

With the quantum chemical calculations

for SnO<sub>2</sub> and doped SnO<sub>2</sub> unit cells, a new model of conductivity in the doped SnO<sub>2</sub>-base inert anode for the electrowinning of aluminum is derived by analysing the compositions of frontier molecular orbitals. It is proposed that the conductivity of the SnO<sub>2</sub>-base inert anode doped by Sb<sub>2</sub>O<sub>3</sub>, ZnO, MnO<sub>2</sub>, TiO<sub>2</sub>, Co<sub>2</sub>O<sub>3</sub> or IrO<sub>2</sub> is raised. Most of the predictions about the effect of the dopants on the conductivities of the anodes are checked with literature data and our experimental results.

## REFERENCES

- Xu, E. J. *et al.* *J. of North East University of Technology*, 1990, 11(4), 362.
- Wang, H. Z. *et al.* *Gansu Nonferrous Metallurgy*, 1989, 3, 63.
- Pople, J. A. *et al.* *Approximate Molecular Orbital Theory*, McGraw-Hill, 1970.
- Research Section of Minerals of Wuhan Institute of Geology. *Crystallography and Mineralogy*, Vol. 2. Geology Press, 1970.
- Plane, R. A. *et al.* (ed). *Physical Inorganic Chemistry*. Benjamin, W. A. Inc, 1963.
- Samsonov, G. V. *The Oxide Handbook*, 2nd. IFI/Plenum Data Company, 1982.
- Yang, J. H. *Doctoral Thesis of the Central-South University of Technology*, 1992.
- Rao, C. N. *et al.* *New Directions in Solid State Chemistry: Structure, Synthesis, Properties, Reactivity and Materials Design*. Cambridge University Press, 1986.