

## Ligand selection for complex-leaching valuable metals in hydrometallurgy

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Received 6 July 2009; accepted 19 November 2009

**Abstract:** A two-stage ligand selection method composed of a primary selection and a critical selection, for complex-leaching valuable metals was presented. At the primary selection stage, three conditions were discussed under a supposed ideal state by mathematical derivation. Generally, ligands selected under condition I were easier for complex-leaching valuable metals than that under condition II, however, under condition III, ligands selected were hard to complex-leaching the valuable metals. Ligands that were out of these three conditions could be disposed directly. In critical selection, ligands selected in primary selection can be finalized. Case applications were provided for verifying the method. The application indicated that iminodiacetate ( $\text{Ida}^{2-}$ ) can be used as a complex agent for complex-leaching smithsonite ( $\text{ZnCO}_3$ ); the leaching condition should be controlled with pH 8–11; the relative error of the minimum consumption of  $\text{Ida}^{2-}$  between the predicted and the calculated results is 5.3%. The results indicate that the theoretical derivations in the ideal state are reliable, and the method for ligand selection is practical and operable.

**Key words:** ligand selection; complex-leaching; smithsonite; hydrometallurgy

## 1 Introduction

Nowadays, with the depletion of copper, zinc sulphuric ores are easily upgraded by floatation. However, the low grade oxide ores are difficult to be upgraded and smelt, which draws more and more attention and thus various hydrometallurgical methods have been developed to leach these low grade oxide ores. The processes include bioleaching, acid leaching, and alkaline leaching. In bioleaching[1–2] bacteria are used to leach ores. It is reported that the bacteria are difficult to be domesticated for the low metals recovery and slow reaction rate, which constrains the development of this process. Acid leaching[3–5] occurs in the acidic media. As we all know, impurities such as Ca, Mg, Fe and Si can be dissolved in these media, which contaminate the leaching liquor and consume leaching reagent. Si is always formed as silica gels in the system and affects the slurry filtration. This limits the process development. Recently, more and more studies focus on the alkaline leaching process in which valuable metals can be selectively separated with impurities by the formation of complexes. Alkaline leaching mainly contains ammonia leaching and caustic soda leaching by using different ligands.  $\text{NH}_3$  is used as a leaching ligand to coordinate

with valuable metal ions ( $\text{Cu}^{2+}$ ,  $\text{Zn}^{2+}$ ) in ammonia leaching. In this process, ammonia evaporates, which causes the environment pollution. Current studies[6–8] still focus on utilizing ammonium to substitute part of ammonia to alleviate the environmental problem. Referring to caustic soda leaching[9–10],  $\text{OH}^-$  is used as a leaching ligand to coordinate with metal ions. The ligand ( $\text{OH}^-$ ) and the metal ion ( $\text{Zn}^{2+}$ ) are combined to form the 4th complex  $\text{Zn}(\text{OH})_4^{2-}$  with high concentrated caustic soda in the solution, which requires large consumption of leaching reagent. While increasing the concentration of  $\text{NaOH}$ ,  $\text{SiO}_2$  in the ore can be dissolved into the solution, which consumes more  $\text{NaOH}$ . The reasons mentioned above constrain the process development. Moreover, because the improper ligands used in the alkaline leaching process seriously affect the mineral resources utilization, it is urgent to study new ligands (or leaching reagents) to treat these low grade oxide ores, which is of great strategic significance for effective utilization and sustainable development of nonferrous metals.

The primary purpose of complex-leaching is to selectively separate valuable metals with impurities by generating complexes. And the main purpose is to dissolve the valuable metals Cu and Zn in leaching liquor and leave the impurities, such as Ca, Mg, Fe and Si in

residue. Because the valuable metals in the oxide ore are mainly in form of carbonates, basic carbonates are insoluble compounds. The recovery of valuable metals by complex-leaching can be achieved by dissolving these insoluble compounds thermodynamically. The dissolving process for insoluble compounds is common in hydrometallurgical and chemical fields. Studies about ligand selection for dissolving the insoluble compound have not been reported in any of the studies published, only some studies[11–13] about leaching insoluble compounds with specific ligand were reported.

In this work, the thermodynamic equilibrium of  $M_aA_m$  (insoluble compounds) dissolved by ligand in aqueous solution was analyzed. It is found that the independent complexation of the ligand with the metal ion M is a key factor to dissolve  $M_aA_m$ . Other factors could be simplified in a supposed ideal state. In this ideal state, the improper ligands could be directly rejected during primary selection, while the remained ligands could be selected carefully using the critical selection method in which all factors were considered. This ligand selection methodology provided fundamentals for studying new leaching reagents in hydrometallurgy.

For the sake of simplification, redox reaction of metal ions and the probable charge were not discussed in this work. The insoluble compounds were symbolised as  $M_aA_m$ , and the ligand was symbolized as L. For metal ion or ligand concentration in aqueous solution, there are two expressions, the total concentration and free concentration, which are unified as  $[M]_T$  and  $[M]$ , respectively.

## 2 Thermodynamic equilibrium and calculation

### 2.1 Thermodynamic equilibrium

#### 2.1.1 Solubility equilibrium of $M_aA_m$

The solubility equilibrium of  $M_aA_m$  is the basis of complex-leaching process. The corresponding reaction is as follows:



Its solubility product constant can be written as

$$K_{sp} = [M]^a[A]^m \quad (2)$$

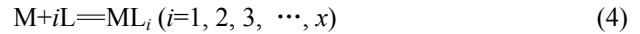
According to Eq.(1), there will be

$$[A]_T = \frac{m}{a} [M]_T \quad (3)$$

#### 2.1.2 Equilibrium of M

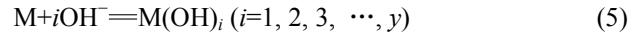
The formation of polynuclear complex and mixed-ligands complex were not considered in the dissolution of  $M_aA_m$ , so reactions in aqueous solution will be simplified as follows:

1) Complex reaction of M with L



$$\beta_{L_i} = \frac{[ML_i]}{[M][L]^i}$$

2) Complex reaction of M with  $OH^-$



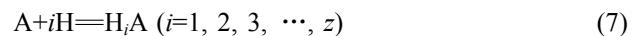
$$\beta_{(OH)_i} = \frac{[M(OH)_i]}{[M][OH^-]^i}$$

The complexation of A with M can be neglected without addition of A. Thereby, the total concentration of M can be expressed as

$$[M]_T = [M] \left( 1 + \sum_{i=1}^x \beta_{L_i} [L]^i + \sum_{i=1}^y \beta_{(OH)_i} [OH^-]^i \right) \quad (6)$$

#### 2.1.3 Equilibrium of A

The protonation of A occurs if A is a weak acid radical in the solution:



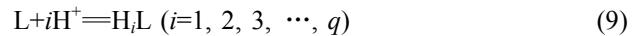
$$\beta_{H_iA} = \frac{[H_iA]}{[A][H^+]^i}$$

The total concentration of A can be expressed as

$$[A]_T = [A] \left( 1 + \sum_{i=1}^z \beta_{AH_i} [H^+]^i \right) \quad (8)$$

#### 2.1.4 Equilibrium of L

The protonation of L can be described as



$$\beta_{LH_i} = \frac{[H_iL]}{[L][H^+]^i}$$

According to Eqs.(4) and (9), the total concentration of L can be expressed as

$$[L]_T = [L] \left( 1 + \sum_{i=1}^x \beta_{L_i} [L]^i + \sum_{i=1}^q \beta_{LH_i} [H^+]^i \right) \quad (10)$$

#### 2.1.5 Dissociation equilibrium of $H_2O$

In aqueous solution, there is always the following equilibrium:

$$K_w = [H^+][OH^-] \quad (11)$$

$K_w$  is a constant when the temperature and pressure are given.

## 2.2 Calculation

There are eight unknown numbers containing  $[M]_T$ ,  $[M]$ ,  $[L]_T$ ,  $[L]$ ,  $[A]_T$ ,  $[A]$ ,  $[OH^-]$ ,  $[H^+]$  in Eqs.(2), (3), (6), (8), (10) and (11). Constants in these equations can be obtained in handbooks of thermodynamic data or by calculation. While the leaching conditions, such as the pH value and  $[L]_T$  value, are fixed, the other six

unknown numbers can be calculated theoretically. This is a methodology for calculating solubility of  $M_aA_m$ . YANG and QIU[14] introduced the similar method. Obviously, the solubility calculated by this method is a comprehensive action of all the factors.

### 3 Ligand selection

It is known to all that there are multiple choices to select ligands which can complex with the metal ion M. It is necessary to select ligands (or leaching reagents) before conducting experiments to recover valuable metal M in oxide ores.

#### 3.1 Primary selection

##### 3.1.1 Independent complexation of ligand

It is said that the solubility of  $M_aA_m$  in  $L-H_2O$  system which has been introduced in section 2.2 is a comprehensive action of all the factors. Actually, under a certain condition, some of the factors that have little influence on the solubility  $M_aA_m$  can be neglected for simplifying the calculation. Especially in selecting ligands, this simplification is necessary and can make primary selection efficient.

To determine whether a ligand is suitable for complex-leaching, it is necessary to exhibit its combining ability completely. Otherwise, the reason why the insoluble compound cannot be dissolved in the solution will be confused. Supposed an ideal state in the system, there is none but the independent complexation of L with M. The total concentration of L is enough to ensure that the metallic ions M are combined to form the most stable complex with L. In this state, the insoluble compound  $M_aA_m$  will be leached certainly by an arbitrary ligand which can complex with M. The consumption of the ligand (the total concentration of L) can be a criterion for ligand selection.

##### 3.1.2 Derivation in ideal state

In the ideal state, the cumulative stable constant of the complex can be written as  $(\beta_{L_i})_{\max}$ . Setting the solubility of  $M_aA_m$  as  $S$ , there will be equilibrium equations as follows:

$$[M]_T = aS = [M](1 + (\beta_{L_i})_{\max}[L]^i) \approx [M](\beta_{L_i})_{\max}[L]^i \quad (12)$$

$$[A]_T = [A] = mS \quad (13)$$

$$[L]_T = [M]i(\beta_{L_i})_{\max}[L]^i + [L] \quad (14)$$

According to Eqs.(12)–(13), there will be

$$[M]^a((\beta_{L_i})_{\max}[L]^i)^a[A]^m = a^a S^a m^m S^m \quad (15)$$

According to solubility product rule of  $M_aA_m$ ,

Eq.(15) can be written as

$$K_{sp} \{(\beta_{L_i})_{\max}[L]^i\}^a = a^a m^m S^{a+m} \quad (16)$$

From Eq.(16), following expression can be obtained:

$$(\beta_{L_i})_{\max}[L]^i = K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}} \quad (17)$$

Inserting Eq.(12) into Eq.(14), an equation can be deduced as follows:

$$[L]_T - iaS = [L] \quad (18)$$

Inserting Eq.(18) into Eq.(17),  $(\beta_{L_i})_{\max}$  can be described as

$$(\beta_{L_i})_{\max} = \frac{K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}}{([L]_T - iaS)^i} \quad (19)$$

In Eq.(19),  $(\beta_{L_i})_{\max}$  can be constrained in a range with the constraint of  $[L]_T$ . Deducing the range of  $(\beta_{L_i})_{\max}$  by discussing the range of  $[L]_T$  using Eq.(19), so, three conditions can be deduced as a result.

I)  $0 < [L]_T - iaS \leq 1$ ,  $(\beta_{L_i})_{\max}$  must satisfy

$$(\beta_{L_i})_{\max} \geq K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}$$

II)  $1 \leq [L]_T - iaS \leq 10$ ,  $(\beta_{L_i})_{\max}$  must satisfy

$$\frac{K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}}{10^i} \leq (\beta_{L_i})_{\max} \leq K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}$$

III)  $10 \leq [L]_T - iaS \leq 100$ ,  $(\beta_{L_i})_{\max}$  must satisfy

$$\frac{K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}}{10^{2i}} \leq (\beta_{L_i})_{\max} \leq \frac{K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}}{10^i}$$

From the view of mathematics, the range of  $[L]_T$  must contain  $[L]_T - iaS \leq 0$ ,  $[L]_T - iaS \geq 100$ . In practice, the range of  $[L]_T - iaS \leq 0$  is not existent, and the range of  $[L]_T - iaS \geq 100$  has no meaning to dissolve  $M_aA_m$  in so high concentration of ligands. While doing primary selection, ligands whose  $(\beta_{L_i})_{\max}$  satisfies condition I should be selected priorly, then condition II, and the last one is condition III. Ligand whose  $(\beta_{L_i})_{\max}$  does not satisfy any one of the three conditions can be deserted directly. In addition, the total concentration of L can be calculated approximately as

$$[L]_T = \left( \frac{K_{sp}^{-\frac{1}{a}} a m^{\frac{m}{a}} S^{\frac{a+m}{a}}}{(\beta_{L_i})_{\max}} \right)^{\frac{1}{i}} + iaS \quad (20)$$

### 3.2 Critical selection

The remained ligands that had been selected by primary selection should be selected carefully in this section. According to the calculation method in section 2.2 with fixed value of pH and  $[L]_T$ , the other unknown numbers can be calculated from the six equilibrium equations. Drawing a 3D graph using pH,  $[L]_T$ , and  $[M]_T$  as coordinates, the change tendency of  $[M]_T$  can be represented apparently with the change of pH and  $[L]_T$ . The ligand should be finally determined in thermodynamics from the analysis of the 3D graph. In addition, the distribution of M and L can help us to analyze the affections of all the factors in dissolving process.

Actually, factors that affect ligand selection are variable. Factors such as the combining ability of the ligand with impurities, the price of the ligand, and the environmental factors of the ligand which are commonly used in hydrometallurgy need to be considered during selection.

## 4 Case application

A sample of a low-grade zinc oxide ore, needs to be leached for recovery of valuable metal Zn. The main phase of Zn is smithsonite ( $ZnCO_3$ ) in the sample, as such we take  $ZnCO_3$  as the insoluble compound for ligand selection.

**Table 1** Requirements of  $(\beta_{L_i})_{\max}$  composing certain level complex

Level	Condition I	Condition II	Condition III
1	$\lg(\beta_{L_i})_{\max} \geq 9.34$	$8.34 \leq \lg(\beta_{L_i})_{\max} \leq 9.34$	$7.34 \leq \lg(\beta_{L_i})_{\max} \leq 8.34$
2	$\lg(\beta_{L_i})_{\max} \geq 9.34$	$7.34 \leq \lg(\beta_{L_i})_{\max} \leq 9.34$	$5.34 \leq \lg(\beta_{L_i})_{\max} \leq 7.34$
3	$\lg(\beta_{L_i})_{\max} \geq 9.34$	$6.34 \leq \lg(\beta_{L_i})_{\max} \leq 9.34$	$3.34 \leq \lg(\beta_{L_i})_{\max} \leq 6.34$
4	$\lg(\beta_{L_i})_{\max} \geq 9.34$	$5.34 \leq \lg(\beta_{L_i})_{\max} \leq 9.34$	$1.34 \leq \lg(\beta_{L_i})_{\max} \leq 5.34$

**Table 2** Results of primary selection

L	Level	$\lg(\beta_{L_i})_{\max}$	Result	L	Level	$\lg(\beta_{L_i})_{\max}$	Result
$OH^-$	4	14.8	I	Glycine(HL)	3	12.33	I
$NH_3$	4	9.46	I	Alanine(HL)	3	10.57	I
$Cl^-$	2	0.61	–	DL-2-aminobutanoic acid (HL)	2	8.65	II
$CN^-$	4	19.62	I	2-amino-2-methylpropanoic(HL)	2	8.60	II
$SCN^-$	4	1.60	III	DL-2-amino-3-butenoic acid(HL)	2	8.86	II
$P_2O_7^{4-}$	2	11.00	I	$\beta$ -alanine(HL)	3	10.40	I
$SO_4^{2-}$	1	2.30	–	Aminomalonic acid(H <sub>2</sub> L)	1	6.48	–
$S_2O_3^{2-}$	1	2.29	–	Aspartic acid(H <sub>2</sub> L)	2	10.15	I
Valine(HL)	3	10.78	I	Glutamic acid(H <sub>2</sub> L)	3	9.80	I
Serine(H <sub>2</sub> L)	3	11.91	I	Homoserine(H <sub>2</sub> L)	2	7.97	II
IDA(H <sub>2</sub> L)	2	12.52	I	Threonine(H <sub>2</sub> L)	2	8.66	II

### 4.1 Primary selection process

At 298 K, the solubility product constant of  $ZnCO_3$  is  $K_{sp}=1\times 10^{-10}$ . Given that  $S=0.469$  mol/L ( $[Zn^{2+}]_T=30$  g/L), the complex levels  $i$  are 1–4. The requirements of  $(\beta_{L_i})_{\max}$  are given in Table 1. Part of the common inorganic ligands and amino acidic ligands was investigated, and the results are given in Table 2.

Table 2 shows that  $(\beta_{L_i})_{\max}$  of ligands  $Cl^-$ ,  $SCN^-$ ,  $SO_4^{2-}$ ,  $S_2O_3^{2-}$  and aminomalonic acid does not satisfy any of the three conditions, so they can be deserted directly.  $(\beta_{L_i})_{\max}$  of inorganic ligands  $OH^-$ ,  $NH_3$ ,  $CN^-$  and  $P_2O_7^{4-}$  satisfy condition I. It seems that they all can be remained for the critical selection.  $NH_3$  and  $CN^-$  which are toxic to human beings and environment will be deserted.  $OH^-$  and  $Zn^{2+}$  are combined together to form its 4th complex which needs the total concentration of  $OH^-$  to be above 1.876 mol/L. Meanwhile,  $SiO_2$  in the ore can be dissolved into the solution at this concentration of  $OH^-$ , which causes more consumption of  $OH^-$ . So, the remained ligand is  $P_2O_7^{4-}$ .

All the amino acidic ligands seem to be remained except for aminomalonic acid ligand. It is known that the price of organic agents is generally expensive. The economic factors should be adequately considered while carrying on the primary selection of these amino acidic ligands. While the specific price of these ligands is unknown, according to Eq.(20), ligand whose  $(\beta_{L_i})_{\max}$  satisfies the condition I and the complex level is lower

can be selected priorly. So, the remained ligands are IDA and Aspartic acid.

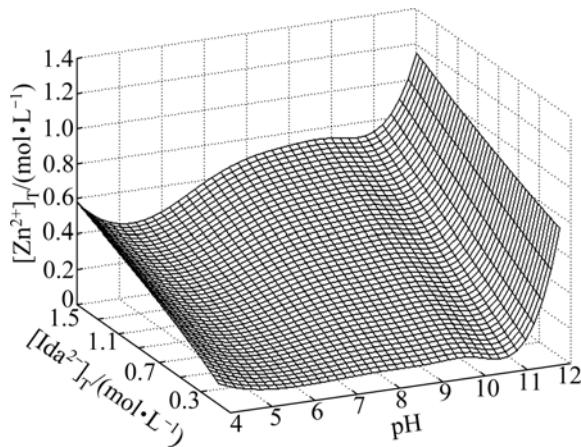
#### 4.2 Critical selection process

Taking IDA ( $C_4H_7O_4N$  iminodiacetic acid) as an example for critical selection, the ligand of IDA can be written as  $Ida^{2-}$ . The thermodynamic data[15–17] are given in Table 3.

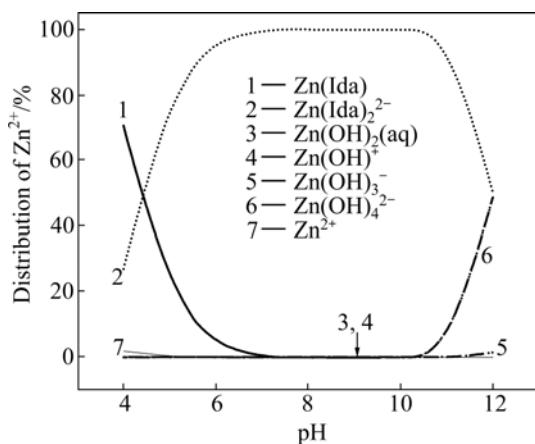
**Table 3** Thermodynamic data of related species at 298 K

Species	$lg\beta_i$	Species	$lg\beta_i$	Species	$lg\beta_i$
$Zn(Ida)$	7.24	$Zn(OH)_3^-$	14.14	$HIda^-$	9.34
$Zn(Ida)_2^{2-}$	12.52	$Zn(OH)_4^{2-}$	17.66	$H_2Ida$	11.95
$Zn(OH)^+$	4.40	$HCO_3^-$	9.57	$H_3Ida^+$	13.77
$Zn(OH)_2(aq)$	11.30	$H_2CO_3(aq)$	15.59		

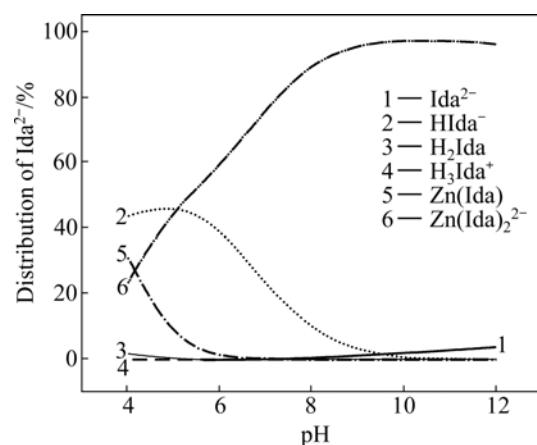
Unknown numbers were calculated and a 3D graph (Fig.1) was given by MATLAB software. When the total concentration of the ligand is 1.0 mol/L ( $[Ida^{2-}]_T=1.0$  mol/L), the distributions of  $Zn^{2+}$ ,  $Ida^{2-}$  and  $CO_3^{2-}$  are represented in Figs.2–4, respectively. The distribution is described as its concentration that occupied in the total concentration. This helps us to understand Fig.1 better.



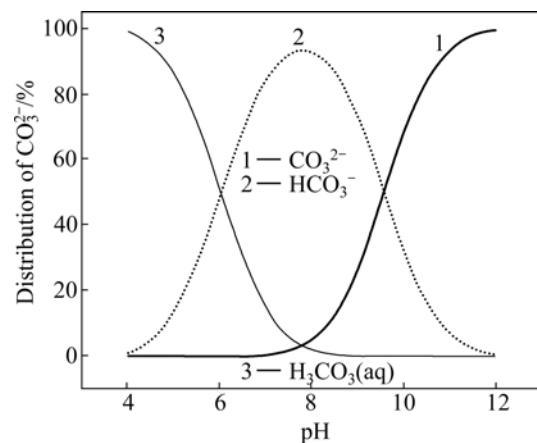
**Fig.1** Tendency of  $[Zn^{2+}]_T$  with pH and  $[Ida^{2-}]_T$



**Fig.2** Distribution of  $Zn^{2+}$  vs pH



**Fig.3** Distribution of  $Ida^{2-}$  with pH



**Fig.4** Distribution of  $CO_3^{2-}$  with pH

Fig.1 shows that the  $[Zn^{2+}]_T$  decreases with the increase of pH value between 4 and 5. While in Fig.2 with pH of 4–5, the distribution of free  $Zn^{2+}$  decreases, meaning that acid-leaching action of  $ZnCO_3$  decreases with the decrease of acidity. While in Fig.3 with pH of 4–5, the distribution of  $HIda^-$  increases, which causes the complexation of  $Ida^{2-}$  with  $Zn^{2+}$  decreasing. Because of these two decreasing actions, the  $[Zn^{2+}]_T$  decreases.

Fig.1 shows that the  $[Zn^{2+}]_T$  increases with the increase of pH value between 5 and 9.6, and then decreases slightly till pH nearly reaches 11.  $[Zn^{2+}]_T$  approaches the highest value when pH reaches 9.6. Fig.2 shows that  $Zn(Ida)$  decreases and  $Zn(Ida)_2^{2-}$  increases till pH=7. In the pH range of 7–11, above 99% of Zn are  $Zn(Ida)_2^{2-}$ . In Fig.3,  $HIda^-$  decreases and  $Zn(Ida)_2^{2-}$  increases strongly from pH 5 to 9; from pH 9 to 11, above 98% of  $Ida^{2-}$  are combined with  $Zn^{2+}$  as  $Zn(Ida)_2^{2-}$ .

From Figs.2 and 3, it seems that the  $[Zn^{2+}]_T$  will not change much from pH 9 to 11. In fact, after the pH value approaches nearby 9.6 in Fig.1,  $[Zn^{2+}]_T$  decreases slightly. The change of this decrease can be explained in Fig.4. In Fig.4, the protonation of  $CO_3^{2-}$  is dominant when pH <

9.6, which is promotional to dissolve  $ZnCO_3$ ; after pH approaches 9.6, the free  $CO_3^{2-}$  becomes dominant.  $[CO_3^{2-}]$  increases dramatically when  $pH > 9.6$ , which causes the decline of  $[Zn^{2+}]$  because of solubility product rules. The decrease of  $[Zn^{2+}]$  causes a slight decrease of  $[Zn^{2+}]_T$ .

Fig.1 shows that  $[Zn^{2+}]_T$  increases sharply with the raise of pH value between 11 and 12. In Fig.2, with the pH of 11–12,  $Zn(Ida)_2^{2-}$  decreases strongly, while  $Zn(OH)_4^{2-}$  increases strongly. Both  $Ida^{2-}$  and  $OH^-$  complex with  $Zn^{2+}$  causing the increase of  $[Zn^{2+}]_T$ . When  $pH > 11$  in Fig.3,  $Zn(Ida)_2^{2-}$  decreases slightly, and free  $Ida^{2-}$  increases slightly. From Figs.2 and 3, it can be predicted that the complexation of  $OH^-$  would replace the complexation of  $Ida^{2-}$  gradually after pH approaches 11, and the consumption of total concentration of  $OH^-$  would be more higher because of its 4th complex with  $Zn^{2+}$ .

In addition, when we use the Eq.(20) to predict the minimum consumption of  $[Ida^{2-}]_T$ , the calculation result is 0.938 mol/L less than 0.99 mol/L ( $pH=9.6$ ,  $[Zn]_T=0.469$  mol/L) in Fig.1. The relative error is only 5.3%. When pH ranges from 9 to 11, the complexation of  $OH^-$  with  $Zn^{2+}$ , the pronation of  $CO_3^{2-}$  and the protonation of  $Ida^{2-}$  can be neglected. The complexation of  $Ida^{2-}$  with  $Zn^{2+}$  can be regarded as the only action in this condition. This proves that the independent complexation of L with M is existent in practice.

Therefore,  $Ida^{2-}$  can be used as a complex agent to leach the sample, and the pH value must be controlled within the range of 8–11.

## 5 Conclusions

1) The key factor for ligand selection is independent complexation of the ligand.

2) The method of ligand section contains primary selection and critical selection. In primary selection, ligands selected under condition I are more easily for complex-leaching valuable metals than that under condition II, and ligands selected under condition III are hard to complex-leach the valuable metals. Ligands that are out of these three conditions can be deserted directly. Ligands selected in primary selection will be finally determined in critical selection.

3) Case application indicates that  $Ida^{2-}$  can be used as a complex agent complex-leaching smithsonite, and pH should be controlled to be 8–11. The relative error of the minimum consumption of  $Ida^{2-}$  between predicted and calculated results is 5.3%.

4) It has been proved that independent complexation

of the ligand is existent in practice, and the theoretical derivations in the ideal state are reliable.

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(Edited by LI Xiang-qun)