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First-principles investigations of structural, mechanical, electronic and optical properties of U₃Si₂-type AlSc₂Si₂ under high pressure

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Abstract: The structural, elastic, electronic and optical properties for U_3Si_2 -type $AlSc_2Si_2$ compound under pressure were systematically investigated by using the first-principles calculations. The values of elastic constants and elastic moduli indicate that $AlSc_2Si_2$ keeps mechanical stability under high pressure. The mechanical properties of $AlSc_2Si_2$ are compared with those of Al_3Sc . The results indicate that $AlSc_2Si_2$ is harder than Al_3Sc . Anisotropic constant A^U and 3D curved surface of elastic moduli predict that $AlSc_2Si_2$ is obviously anisotropic under pressure. The electronic structure of $AlSc_2Si_2$ exhibits metallic character and the metallicity decreases with the elevated pressure. In addition, optical properties as a function of pressure were calculated and analyzed. The present work provides theoretical support for further experimental work and industrial applications.

Key words: U₃Si₂-type AlSc₂Si₂; mechanical properties; electronic structure; optical properties; first-principles calculations

1 Introduction

The L1₂-type Al₃Sc precipitates can form a stable and fine-grain structure and block the mobile dislocations. The outstanding physical features make Al-based alloys with Sc element have excellent mechanical properties with elevated temperature. Al₃Sc intermetallics have been deemed as an effective strengthening phase in the development of novel Al-based alloys [1–7]. The physical properties of Al₃Sc have been investigated extensively over the past twenty years, such as mechanical properties [8-16], electronic properties [16–20], thermodynamic and optical properties [21-24]. The addition of Si element into Al-Sc alloys reduced the amount of Al₃Sc precipitates. The Al-Si-Sc alloys trend to form the V-phase (AlSc₂Si₂) in the isothermal section of the phase diagram [25]. ZHANG et al [26] used the scanning electron microscopy (SEM) and energy dispersive spectroscopy (EDS) and found that the AlSc₂Si₂ precipitates were adjacent to the grain boundary in the Al-Si-Sc alloys. The AlSc₂Si₂ precipitates have caused significant changes in the microstructure and mechanical properties in the Al–Sc alloys [26,27]. For the physical properties of AlSc₂Si₂, the first-principles calculations have been used to investigate the formation enthalpy, elastic constants and density of states [28]. However, to the best of our knowledge, many physical properties of AlSc₂Si₂ are not well investigated under high pressure. The available reports are not enough to systematically understand the physical properties of AlSc₂Si₂. So, in the present work, the physical properties of AlSc₂Si₂ were systematically investigated by using the first-principles calculations.

2 Computation methods

The present calculations were performed with the first principles method based on the pseudopotential plan-wave within density functional theory (DFT) using Cambridge Serial Total Energy Package (CASTEP) [29] code. Ultrasoft pseudo-potentials were used to model the ion–electron interaction. The exchange and correlation potentials were described with the generalized gradient approximation (PBE-GGA). Pseudo-atomic calculations were performed for Sc $3s^23p^63d^14s^2$, Si $3s^23p^2$ and Al $3s^23p^1$. Tests of the convergence can be obtained with

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cutoff energy of 400 eV and the Monkhorst–Pack special *k*-point scheme with $8 \times 8 \times 14$ grid meshes in the Brillouin zone. We used the Pulay scheme of density mixing for the evaluation of energy and stress. In the meantime, the tolerance of the geometry optimization was set to be less than 5.0×10^{-6} eV/atom. The maximum ionic Hellmann–Feynman force, ionic displacement and stress were 0.001 eV/Å, 0.0005 Å and 0.03 GPa, respectively. We used the tetrahedron Bloch method with corrections to calculate electronic structure. The SCF tolerance was set to be 5.0×10^{-6} eV/atom. The stress–strain method [30] was used to calculate elastic constants of AlSc₂Si₂.

3 Results and discussion

3.1 Structural properties

The ternary compound $AlSc_2Si_2$ has tetragonal U_3Si_2 crystal structure with space group P4/mbm (No. 127). In the unit cell of $AlSc_2Si_2$, Al atom occupies the Wyckoff site 2a (0, 0, 0), Sc atom occupies the Wyckoff site 4h (0.1786, 0.6786, 0.5) and Si atom occupies the Wyckoff site 4g (0.3692, 0.8692, 0), as shown in Fig. 1. The total energy of $AlSc_2Si_2$ as a function of the volume was calculated. The ground state structural parameters and pressure–volume curve can be obtained by fitting the data of energy vs volume to the Birch–Murnaghan equation of state [31], in which the pressure–volume relationship is expressed as

$$P = 3B_0 f_{\rm E} (1 + 2f_{\rm E})^{5/2} \cdot \left\{ 1 + \frac{3}{2} \left[B_0 B'' + (B' - 4)(B' - 3) + \frac{35}{9} f_{\rm E}^2 \right] \right\}$$
(1)

where $f_{\rm E}=1/2[(V_0/V)^{2/3}-1]$, B'=dB/dP and B_0 are hydrostatic bulk modulus, the pressure derivative of the bulk modulus and zero pressure bulk modulus,



Fig. 1 Crystal structure of tetragonal AlSc₂Si₂ (pink balls, yellow balls and blue balls represent Al atoms, Sc atoms and Si atom, respectively)

respectively. The ground state structural parameters are listed in Table 1, along with the available experimental and theoretical values. The calculated results are very close to the values of the available experiments and theoretical calculations [28,32]. This indicates that the computation method is reliable. To investigate the influence of pressure on the crystal structure for AlSc₂Si₂, the curves of the lattice parameters (a/a_0 , c/c_0) and unit cell volume ratio (V/V_0) of AlSc₂Si₂ with pressure are plotted in Fig. 2. The ratios of a/a_0 , c/c_0 and V/V_0 decrease with the increase of pressure. The polynomial function relationships of a/a_0 , c/c_0 and V/V_0 are

$$a/a_0 = 0.9997 - 0.0050P + 1.2281 \times 10^{-4}P^2$$
 (2)

$$c/c_0 = 1.0005 - 0.0091P + 1.2438 \times 10^{-4}P^2$$
 (3)

$$V/V_0 = 1.0002 - 0.0032P + 4.3810 \times 10^{-5}P^2 \tag{4}$$

Equations (2) and (3) reveal that $AISc_2Si_2$ is compressible along *a* axis and *c* axis. In Fig. 2, the ratios of the lattice parameters and volume at 30 GPa decrease by about 9%, 6% and 18%, respectively. However, with the elevated pressure, the distance between atoms becomes smaller due to the stronger repulsive interaction among atoms, which leads to the compression more difficult under high pressure.

Table 1 Calculated lattice constant bulk modulus B_0 and its first pressure derivative B'_0 of AlSc₂Si₂ compared with other theoretical calculations and experiments at 0 GPa

a_0	c_0	B_0	B'_0	Resource
6.603	4.006	100.9	4.02	Present work
6.597	3.994	_	_	Experiment [32]
6.608	4.000	101.6	3.97	Calculation [28]



Fig. 2 Variations of ratios, a/a_0 , c/c_0 and V/V_0 , of AlSc₂Si₂ as function of pressure

3.2 Mechanical properties

For the tetragonal crystalline, $AISc_2Si_2$ has six independent elastic constants, that is, C_{11} , C_{33} , C_{44} , C_{66} , C_{12} and C_{13} . The calculated elastic constants are listed in Table 2 and are consistent with the theoretical values [28]. The calculated elastic constants versus pressure are plotted in Fig. 3. The calculated elastic constants C_{ij} of AlSc₂Si₂ exhibit similar tendency and increase almost linearly with the increasing pressure from 0 to 30 GPa. These elastic constants satisfy traditional mechanical stability conditions [33], C_{11} - C_{12} >0, C_{11} >0, C_{33} >0, C_{44} >0, C_{66} >0, C_{11} + C_{33} - $2C_{13}$ >0, $2(C_{12}+C_{11})+C_{33}+4C_{13}>0$, indicating that AlSc₂Si₂ is mechanically stable for the considered pressure range. In Fig. 3, the elastic constants C_{11} and C_{33} are larger than others in the considered pressure range. This indicates that AlSc₂Si₂ is incompressible under uniaxial stress along the *z* axis or *x* axis.

Table 2 Calculated elastic constants of $AlSc_2Si_2$ at 0 GPa

Resource	C ₁₃ / GPa	C ₁₂ / GPa	C ₆₆ / GPa	C ₄₄ / GPa	C33/ GPa	C ₁₁ / GPa
Present work	56.62	71.24	75.58	97.14	173.65	181.54
Ref. [28]	59.68	65.64	73.94	95.64	170.70	179.41



Fig. 3 Calculated elastic constants, C_{ij} , under different pressures

The mechanical properties are mainly determined by the elastic moduli, including Poisson ratio v, shear modulus G, elastic modulus E and bulk modulus B. These moduli are calculated in term of the elastic constants C_{ij} using the following formulas [34]:

$$B = \frac{1}{2}(B_{\rm V} + B_{\rm R}) \tag{5}$$

$$G = \frac{1}{2}(G_{\rm V} + G_{\rm R}) \tag{6}$$

$$v = \left[\frac{3B - 2G}{6B + 2G}\right] \tag{7}$$

$$E = \frac{9GB}{G+3B} \tag{8}$$

For tetragonal crystal [35]:

$$B_{\rm V} = [2(C_{11} + C_{12}) + C_{33} + 4C_{13}]/9 \tag{9}$$

$$B_{\rm R} = C^2 / M \tag{10}$$

$$G_{\rm V} = (M + 3C_{11} - 3C_{12} + 12C_{44} + 6C_{66})/30 \tag{11}$$

$$G_{\rm R} = 15/[18B_{\rm V}/C^2 + 6/(C_{11} - C_{12}) + 6/C_{44} + 3/C_{66}]$$
(12)

where B_V and G_V are the Voigt's bulk and shear modulus, respectively; B_R and G_R are the Reuss's bulk and shear modulus, respectively. The calculated elastic moduli at 0 GPa are listed in Table 3 along with the available values [28]. The obtained mechanical moduli (B, G, E)of AlSc₂Si₂ under high pressure are plotted in Fig. 4. These moduli also exhibit similar variation tendency and increase almost linearly with increasing pressure from 0 to 30 GPa. In Fig. 4, the values of B are larger than those of G in the whole pressure range. This indicates that the parameter limiting the stability of AlSc₂Si₂ under high pressure is the shear modulus [36]. In Fig. 4, we provide the mechanical data for Al₃Sc [15]. The mechanical properties of U₃Si₂-type AlSc₂Si₂ are compared with those of the cubic Al_3Sc . The elastic moduli B, G, E of AlSc₂Si₂ are all larger than those of Al₃Sc under pressure from 0 to 30 GPa, respectively. The results indicate that AlSc₂Si₂ is harder to compress than Al₃Sc. The value of B/G is related to the brittleness and ductile of materials. The critical value which separates ductile and brittle material is 1.75; i.e., if B/G>1.75, the material behaves in a ductile manner; otherwise, the material will have a brittle manner [32]. In Table 3, we can see that the result of B/G is smaller than 1.75 at 0 GPa, which indicates that AlSc₂Si₂ is the brittle material.

In Fig. 5, the values of B/G of AlSc₂Si₂ increase with the elevated pressure, indicating that the pressure

Table 3 Calculated elastic moduli *B*, *G*, *E*, *v*, *B*/*G* and anisotropy index A^{U} at 0 GPa

<i>B</i> /GPa	G/GPa	E/GPa	v	B/G	A^{U}	Resource
101.27	76.02	176.32	0.211	1.332	0.565	Present work
99.88	74.1	178.23	0.203	1.345	0.567	Ref. [28]



Fig. 4 Bulk modulus, shear modulus and elastic modulus under different pressures

can reduce the brittleness of $AlSc_2Si_2$. Figure 5 also provides the relationship between Poisson ratio and pressure. The values of v increase with the elevated pressure. Poisson ratio v can provide some useful information about the properties of bonding forces. The upper limit for central force of solids is 0.5 and the lower limit is 0.25. In the present work, the value of v is 0.211 at 0 GPa, which is smaller than the lower limit, which indicates that the inter-atomic forces of $AlSc_2Si_2$ are not central forces. The values of v increase with elevated pressure and become beyond the lower limit values of 0.25 under pressure from 15 to 30 GPa, indicating that the inter-atomic forces of $AlSc_2Si_2$ become central forces under pressure from 15 to 30 GPa.



Fig. 5 Calculated Poisson ratio (a) and B/G (b) under different pressures

Elastic anisotropy constant is an important physical parameter of materials and has many industrial and technological applications. Based on the obtained elastic constants and moduli, we calculated universal elastic anisotropy index A^{U} to estimate the anisotropy of AlSc₂Si₂. The universal elastic anisotropy index, A^{U} , was proposed as follows [37]:

$$A^{\rm U} = 5\frac{G_{\rm V}}{G_{\rm R}} + \frac{B_{\rm V}}{B_{\rm R}} - 6 \ge 0 \tag{13}$$

The universal elastic anisotropy index, A^{U} , is equal to zero, namely, the crystal with the value of $A^{U=0}$ is elastically isotropic. At 0 GPa, the A^{U} of AlSc₂Si₂ is 0.565 and obviously deviates from 0, indicating that it is anisotropic. Figure 6 shows the relationship between $A^{\rm U}$ and pressure. The values of A^{U} increase with the elevated pressure. However, the values of A^{U} are in the range of 0.565-0.613 from 0 to 30 GPa and the anisotropic content shows little change. For comparison, the values of A^{U} of Al₃Sc from Duan's work [20] are plotted in Fig. 6. The values of A^{U} are in the range of 0.002–0.0375 from 0 to 30 GPa and are all close to 0, indicating that Al₃Sc basically keeps isotropic in the whole pressure range. In order to further treat the elastic anisotropy, the three-dimensional curved surfaces of elastic modulus in given direction are plotted. The 3D elastic modulus surface can be determined by using the following equations [38,39].



Fig. 6 Anisotropy coefficient A^U of AlSc₂Si₂ and Al₃Sc under different pressures

For cubic crystal structure,

$$\frac{1}{E} = S_{11} - 2\left(S_{11} - S_{12} - \frac{S_{44}}{2}\right)\left(l_1^2 l_2^2 + l_2^2 l_3^2 + l_1^2 l_3^2\right)$$
(14)

For tetragonal crystal structure,

$$\frac{1}{E} = S_{11}(l_1^4 + l_2^4) + (2S_{13} + S_{44})(l_1^2 l_3^2 + l_2^2 l_3^2) + S_{33}l_3^4 + (2S_{12} + S_{66})l_1^2 l_2^2$$
(15)

where S_{ij} is the elastic compliance constant and l_1 , l_2 and l_3 are the direction cosines. For an isotropic crystal, the 3D curved surface would exhibit a spherical shape and the deviation degree from the spherical surface indicates the contents of anisotropy. We calculated elastic compliance constants S_{ij} and obtain the 3D elastic modulus surface. The 3D figures of Al₃Sc and AlSc₂Si₂ at 0 and 30 GPa are plotted in Fig. 7. In Fig. 7, the 3D surfaces of the Al₃Sc at 0 and 30 GPa are obviously in spherical shape and exhibit a noticeable isotropy.



Fig. 7 Directional dependence of elastic modulus for Al₃Sc (a, b) and AlSc₂Si₂ (c, d) under pressures: (a, c) 0 GPa; (b, d) 30 GPa

However, we can note that the deviation degrees from the spherical surface of $AlSc_2Si_2$ are obviously larger than those of Al_3Sc , which indicates that $AlSc_2Si_2$ has stronger anisotropy than Al_3Sc in different directions. In the meantime, the contents of deviation show little change with elevated pressure. These results are also consistent with the analysis of anisotropy factors A^U under pressure.

3.3 Electronic properties

The electronic band structure for AlSc₂Si₂ was calculated using the equilibrium lattice parameters and shown in Fig. 8. The conduction and valence bands obviously overlap and there is no energy gap around the Fermi level, which indicates that AlSc₂Si₂ exhibits a metallic character. The total density of states and partial density of states for AlSc₂Si₂ are shown in Fig. 9. The value of density of states at Fermi energy is nonzero, which also confirms that AlSc₂Si₂ has metallic character. In the meantime, the density of states is mainly dominated by the hybridization of Al 3s, Al 3p and Si 3s states from -11.883 to -6 eV. From -6 eV to 0 eV, the energy binding states are dominated by Al 3p, Si 3p and Sc 3d states. In the conduction region, the electronic structure is also dominated by Al 3s, Al 3p, Si 3p and Sc 3d states. Figure 10 shows the total density of states under pressure. The energy regions around Fermi level are from -11.883 to 4.227 eV, from -12.409 to 4.773eV,



Fig. 8 Band structure of AlSc₂Si₂ at 0 GPa



Fig. 9 Partial and total density of states of AlSc₂Si₂ at 0 GPa



Fig. 10 Total density of states of AlSc₂Si₂ at different pressures

from -12.801 to 5.152, and from -13.095 to 5.398 eV at 0, 10, 20 and 30 GPa, respectively. In Fig.10, the profile of total density of states shows little changes, which means that the structure of AlSc₂Si₂ keeps structural stability up to 30 GPa. Moreover, the total density of states decreases with the elevated pressure. The calculated values of the total density of states at Fermi level are 3.255, 2.957, 2.946 and 2.898 state/eV at 0, 10, 20 and 30 GPa, respectively. This is because the distance between atoms under high pressure becomes smaller and gives rise to the change of the interaction potentials. A pseudo-gap exists around Fermi level and pseudo-gaps become wider with the elevated pressure. It is concluded that the covalent bond increases with the elevated pressure. Generally speaking, the wider pseudo-gap represents the stronger covalent bond [40]. In the meantime, we also estimate the metallicity of AlSc₂Si₂ compound by following equation [41]: $f_{\rm m}=0.026D_{\rm f}/n_{\rm e}$, where $n_{\rm e}$ is the valence electron density of the cell and $D_{\rm f}$ is the value of the density of states at Fermi level. The calculated values of f_m are 0.1138, 0.1052, 0.1023 and 0.1005, at 0, 10, 20 and 30 GPa, suggesting that the metallicity of AlSc₂Si₂ decreases with elevated pressure.

3.4 Optical properties

To further investigate the physical properties, the optical parameters are calculated, including the dielectric function $\varepsilon(\omega)$, the refractive index $n(\omega)$ and the extinction coefficient $k(\omega)$. These optical parameters can be obtained by the complex dielectric function $\varepsilon(\omega)$: $\varepsilon(\omega)=\varepsilon_1(\omega)+i\varepsilon_2(\omega)$. $\varepsilon_1(\omega)$ and $\varepsilon_2(\omega)$ are the real part and imaginary part of the complex dielectric function. The refractive index $n(\omega)$ and $\varepsilon_2(\omega)$, are calculated through the following equations [42]:

$$n(\omega) = \left[\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} + \varepsilon_1(\omega)\right]^{1/2} / \sqrt{2}$$
(16)

$$k(\omega) = \left[\sqrt{\varepsilon_1^2(\omega) + \varepsilon_2^2(\omega)} - \varepsilon_1(\omega)\right]^{1/2} / \sqrt{2}$$
(17)

Figures 11 and 12 provide the optical properties in the energy range of 0-20 eV. There are no experimental data for AlSc₂Si₂. The calculated results will provide theoretical support for further experimental work and industrial applications. In Fig. 11, the values of the real part and imaginary part are close to zero and change very little in a high energy region. The main peak of imaginary part appears around 0.97 eV and originates predominantly from the direct optical transitions between Sc 3d states and Al 3s states. The curve of the real part declines linearly with elevated energy from 0 to 4 eV. Figure 12 shows the calculated refractive index $n(\omega)$ and extinction coefficient $k(\omega)$ for AlSc₂Si₂. Generally speaking, the square of refractive index $n(\omega)$ is proportional to dielectric constant $\varepsilon_1(\omega)$. Larger dielectric constant represents larger refractive index. So, the shape of curves of the refractive index $n(\omega)$ and dielectric constant $\varepsilon_1(\omega)$ is similar to each other. The main peak of extinction coefficient $k(\omega)$ appears around 2.75eV and then declines linearly with elevated energy to 12.7 eV.



Fig. 11 Real part and imaginary part of dielectric function for AlSc₂Si₂



Fig. 12 Calculated refractive index and extinction coefficient for $AlSc_2Si_2$

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The pressure effects on static dielectric constant $\varepsilon_1(0)$ and static refractive index n(0) for AlSc₂Si₂ are shown in Fig. 13. In Fig. 13, these parameters increase or decrease monotonically with increasing pressure from 0 to 30 GPa. We fit the calculated data to the quadratic polynomial and obtain the relationship between $\varepsilon_1(0)/n(0)$ and pressure:

 $\varepsilon_1(0) = 76.672 + 0.626P - 0.0307P^2 \tag{18}$

$$n(0) = 8.779 - 0.0368P - 0.0018P^2 \tag{19}$$



Fig. 13 Pressure dependence of static dielectric constant $\varepsilon_1(0)$ (a) and static refractive index n(0) (b) for AlSc₂Si₂

Generally speaking, simple relationship а empirically links the mechanical properties of materials with their elastic modulus. The bulk modulus represents the resistance to volume change under pressure. The shear modulus represents the resistance to shape change caused by shearing force. In the meantime, the shear modulus plays more important role in determining the hardness of material. Elastic modulus is also a very important constant for the mechanical properties of materials. In Fig. 4, the values of the elastic moduli, B, G and E, of $AlSc_2Si_2$ are larger than those of Al_3Sc_2 indicating that AlSc₂Si₂ is harder to compress than Al₃Sc. $AlSc_2Si_2$ is the better strengthening phase than Al_3Sc . Meanwhile, Si element is cheaper than Sc, so adding Si to Al–Sc alloys can reduce the production costs of Al–Sc alloys.

4 Conclusions

1) The calculated structural data are very close to the values of the available experiment and calculation. The ratios of structural parameters a/a_0 , c/c_0 and V/V_0 decrease with the increasing pressure.

2) AlSc₂Si₂ keeps mechanically stable under pressure from 0 to 30 GPa. The values of *B*, *G* and *E* under pressure increase with elevated pressure, suggesting that the crystal structure of AlSc₂Si₂ becomes more and more difficult to change with elevated pressure. The calculated anisotropic constants A^{U} and 3D curved surface of elastic modulus show that AlSc₂Si₂ is obviously anisotropic for considered pressure.

3) The calculated electronic structure shows that the $AlSc_2Si_2$ exhibits metallic character and keeps structural stability from 0 to 30 GPa. The pseudo-gap illustrates that the capacity of covalent bond becomes stronger.

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高压下 U₃Si₂型 AlSc₂Si₂ 金属间化合物的 结构、力学、电子结构和光学特性的 第一性原理计算

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摘 要:通过第一性原理方法计算了高压下 AlSc₂Si₂ 金属间化学物的结构、力学、电子和光学特性。计算的弹性 常数及模量表明 AlSc₂Si₂ 在高压下保持良好的力学稳定性。将 AlSc₂Si₂ 和 Al₃Sc 的力学性能对比发现,AlSc₂Si₂ 较 Al₃Sc 有更高的硬度。各向异性常数和 3D 弹性模量图像表明 AlSc₂Si₂ 是各向异性材料。电子结构特性表明 AlSc₂Si₂ 具有金属的性质并且这种性质随着压力的升高而减弱。同时计算和分析了其光学性质与压强的关系。这 些计算结果为进一步的实验工作提供了理论支持。

关键词: U₃Si₂型 AlSc₂Si₂; 力学性能; 电子结构; 光学性质; 第一性原理计算

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