

Size and shape effects on Curie temperature of ferromagnetic nanoparticles

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Abstract: A simplified model was developed to describe the Curie temperature suppression of ferromagnetic nanoparticles. Based on a size and shape dependent model of cohesive energy, the critical temperature variations of ferromagnetic nanoparticles were deduced. It is predicted that the Curie temperature of nanoparticles depends on both size and shape conditions, among which the temperature suppression is strongly influenced by the particle size and the shape effect is comparably minor. The calculation values for freestanding nanoparticles are in good agreement with other theoretical model and the experimental results. The model is also potential for predictions for the nanoparticles embedded in different substrates.

Key words: nanoparticle; size effect; shape effect; ferromagnet; Curie temperature

1 Introduction

In recent years, ferromagnetic nanoparticles have been extensively investigated due to their scientific and industrial importance, and unique properties resulting from their ultrafine sizes. It has been reported that when the size reduces to a nanometer, ferromagnetic solids may exhibit superparamagnetism[1], higher coercive force[2], giant magnetoresistance[3], phase transformation[4] and lower Curie temperature[5–9]. The last point of Curie temperature T_C suppression, namely, T_C of ferromagnetic nanoparticles decreases with decreasing diameter, is quite interesting for the development of new functional materials, such as switches functioning in a designed temperature range with tunable T_C , temperature sensitive ferromagnets applied in magnetic fluids[10].

Some models have been developed to understand the experimental observations of T_C suppression. The first one should be mentioned is the scaling theory established by FISHER and BARBER[6] for finite-size effects in ferromagnetic systems. Based on the spin-spin correlation length (SSLC, ξ) mechanism, it is predicted that if the nanosolid size is smaller than the critical SSLC, the T_C will shift to a lower temperature $T_C(D)$ than the

bulk value $T_C(\infty)$, and the relationship can be expressed by a step function as

$$\frac{T_C(D)}{T_C(\infty)} = 1 - \left[\frac{\xi + r}{2D} \right]^\lambda \quad (D > \xi) \quad (1)$$

$$\frac{T_C(D)}{T_C(\infty)} = \frac{D - r}{2\xi} \quad (D < \xi) \quad (2)$$

where D is the size of nanocrystals, r denotes the thickness of a monolayer, and λ is the corresponding critical exponent. Though the original model is limited in a thin film system, the pioneering conception strongly impacts general understandings on the Curie temperature suppression. For example, NIKOLAEV and SHIPILIN [11] have proposed a $T_C(D)$ function for ferromagnetic nanoparticles as

$$\frac{T_C(D)}{T_C(\infty)} = 1 - \frac{3\Delta L}{2D} \quad (3)$$

where ΔL is the thickness of surface layer of nanoparticles, characterizing the influence of the surface layer on the Curie temperature in light of exchange bond variations. However, when this model is utilized to fit experimental data for Fe_3O_4 nanoparticles of different

sizes, a constant ΔL is unsuccessful in the full size range of nanometer. This may be caused by the variation of ΔL with the solid size, and the relationship between ΔL and D is expected to be established.

Another approach has been reported by SUN et al [7]. In their work, the bond order-length-strength(BOLS) correlation mechanism is incorporated into the Ising premise to advance a unified expression for T_C predictions of ferromagnetic, ferroelectric and superconductive nanosolids. The lower Curie temperature is related to the decrease of atomic cohesive energy that caused by the coordination number(CN) imperfection of the lower coordinated atoms near the surface edge. In other terms, JIANG et al[8,12] have discussed the size and interface effects on the critical temperatures mentioned above. Based on a size-dependent cohesive energy model, a unified function is modeled to predict the T_C suppression with decreasing nanocrystal size. The same prediction is also obtained in their discussion on the Curie transition temperature of ferromagnetic low-dimensional metals (particles, wires and thin films) with different morphologies in full size range.

All these developed models are significant to understand the nature of T_C suppression of ferromagnetic nanosolids from different perspectives. However, another important aspect of particles, the shape of nanoparticles has not been paid enough attention to in some work. Currently, the shape of nanoparticles is generally regarded as spherical type in thermal calculation, while depending on different production conditions, particles may also exhibit cubic, columnar, polyhedral and other shapes. For a nanoparticle with the same size, different shapes lead to different specific surfaces, which can remarkably influence its physicochemical properties [13–16]. Therefore, variations on the shape of nanoparticles should not be ignored. For a better understanding of both size and shape effects on the Curie temperature variation of ferromagnetic nanoparticles, a simplified model was developed in this work. Based on the cohesive energy model and the relationship between Curie temperature and cohesive energy, the temperature variations for freestanding ferromagnetic nanoparticles were described. The Curie temperature of nanoparticles embedded in substrate films was discussed as well.

2 Model

The Curie temperature is a critical parameter for ferromagnetic nanoparticles, which is determined by the spin-spin exchange interaction. Upon a temperature higher than the Curie point of ferromagnets, the exchange interaction caused by the spin magnetic moment of neighboring 3d electrons will be very weak or

even disappear. At that time, the spin-spin interaction is disordered by thermal stimulus, and ferromagnet becomes paramagnet of magnetic disorder. To destroy the magnetic exchange, sufficient energy has to be provided to break all atomic bonds and promote the atoms for thermal vibration. During this process, the total energy, or exchange interaction energy $E_{\text{exc}}(T)$ can be regarded to equal the sum of the cohesive energy E and the thermal vibration energy $E_v(T)$ needed to disorder the spin-spin interaction, namely,

$$E_{\text{exc}}(T) = E + E_v(T) \quad (4)$$

Based on a mean field approximation, the thermal vibration energy has a proportional relationship with temperature, i.e., $E_v(T) = k_B T$, where k_B is the Boltzmann constant. At Curie temperature, the thermal vibration energy required to disorder the exchange interaction is a portion of the atomic cohesive energy at $T=0$ [7–8, 17–18]. From this point of view, the Curie temperature can be regarded directly proportional to the cohesive energy ($T_C \propto E$) as a first order approximation, since the nature of any phase transition is related with the potentials of the two related phases. As an empirical result,

$$\frac{E_n}{E_b} = \frac{T_{Cn}}{T_{Cb}} \quad (5)$$

where E and T_C denote cohesive energy and Curie temperature, and the subscripts n, b denote nanoparticle, corresponding bulk respectively. According to Eqn.(5), the Curie temperature T_C should have the same size and shape dependence as cohesive energy E . In this term, to figure out the size and shape effects on cohesive energy becomes critical to develop a size and shape dependent model for the Curie temperature of ferromagnetic nanoparticles. This concept is helpful to understand the Curie temperature variations of ferromagnetic nanoparticles, especially for the comparison within the same series of sample system.

3 Results and discussion

3.1 Calculation of cohesive energy

The cohesive energy equals the energy needed to destroy all bonds when dividing the crystal into isolated atoms, namely, the cohesive energy is directly determined by the product of the bond amount and its unit energy [15–16, 19–20]. Supposing the bond energy equals each other for the same atom, the cohesive energy will depend on its bond amount. For nanoparticles, due to the well-known surface effects, the values of cohesive energy are not all the same for the superficial part and interior part, caused by their thermal behavior difference.

One case in point is their atomic relaxation caused by surface coordination-number imperfection[21]. Such a difference for finite particles cannot be ignored, so the cohesive energy of nanoparticles should be the sum of the superficial part and the interior part. Accordingly, we obtain the surface-to-volume atomic ratio dependent expression for cohesive energy of nanoparticles as follows:

$$E_n = (1-\alpha)E_b + \alpha E_s \quad (6)$$

where the subscript 's' represents the surface, α means the surface-to-volume atomic ratio. Supposing the bond amount of interior atom is m , the bond amount of a surface atom with interior atoms is $(1/4)m$ for simplicity. Such opinion is supported by Ref.[22], where the surface relaxation is regarded as only about one-fourth of the area of each surface atom embedded in the lattice. Then we obtain Eqn.(7) for freestanding nanoparticles and Eqn.(8) for embedded nanoparticles[15–16]:

$$\frac{E_n}{E_b} = 1 - \frac{3}{4}\alpha \quad (7)$$

$$\frac{E_n}{E_b} = 1 - \frac{3}{8}\alpha(1 - \eta \frac{E_M}{E_b}) \quad (8)$$

where the subscript M denotes the embedding matrix, η represents the misfit between nanoparticles and matrix. In a case of incoherent interface between nanoparticles and matrix, $\eta=0$; and for a completely coherent interface, $\eta=1$. One point that should be noted is that behaviors between freestanding nanoparticles and embedded ones with incoherent interface are not quite the same. So if set $\eta=0$ in Eqn.(8), $E_n/E_b=1-(3/8)\alpha$ will be obtained for an incoherent interface between particles and matrix, which is not consistent with Eqn.(7) for freestanding nanoparticles. A possible reason for such phenomenon may be that the thermal vibration amplitudes of surface atoms are less than those of interface atoms, which leads to the above different behaviors between freestanding and embedded nanoparticles.

In Eqns.(7) and (8), α denotes surface-to-volume atomic ratio, where the surface details should be noted. Usually, the nanoparticle is simplified as spherical shape for calculation. Then according to the definition, the surface-to-volume atomic ratio can be described as

$$\alpha = \frac{S \cdot d}{V} = \frac{4\pi R^2 \cdot d}{\frac{4}{3}\pi R^3} = \frac{3d}{R} \quad (6)$$

where d is the atom diameter, R is the nanoparticle radius, and the surface is assumed to be shell structure consisting of one layer of atoms. Similarly, supposing the shape of the nanoparticle is ideal cubic, α can be deduced

as

$$\alpha = \frac{8}{n^{1/3} C^{2/3} \pi k^2} \quad (10)$$

where n denotes the atomic number of nanocrystals, C is the atomic number of one structure cell, and k is the ratio between equivalent atomic radius and lattice parameter. For FCC, BCC and HCP structures, C are 4, 2 and 2, and k are $\sqrt{2}/4$, $\sqrt{3}/4$ and $1/2$, respectively [24].

Substituting Eqn.(10) into Eqn.(7), the cohesive energy for freestanding nanoparticles can be described as [23]

$$E_n = E_b \left(1 - \frac{6}{n^{1/3} C^{2/3} \pi k^2} \right) \quad (11)$$

As shape variation is significant to the thermal properties of nanoparticles, a shape factor μ can be defined as the ratio of two surface areas to describe the difference between non-cubic and cubic particles, i.e.,

$$\mu = \frac{S}{S_{\text{cubic}}} \quad (12)$$

where S is the surface area of the particle in random shape, and S_{cubic} is the surface area of the cubic particle, which is supposed to have the same volume as the former. The conception of shape factor is especially practical benefit when the experimental observation of particle shape is combined with theoretical prediction. For example, the particle shape may be determined by the high resolution transmission electron microscopy (HRTEM), then the shape factor can be figured out and used in an exact prediction, such as thermal stability of nanomaterials[16].

Combining Eqns.(11) with (12), the cohesive energy of freestanding nanoparticles with random shape can be described as

$$\frac{E_n}{E_b} = 1 - \frac{6\mu}{n^{1/3} C^{2/3} \pi k^2} \quad (13)$$

Based on the same conception, the cohesive energy of nanoparticles under embedded condition is

$$\frac{E_n}{E_b} = 1 - \frac{3\mu}{n^{1/3} C^{2/3} \pi k^2} (1 - \mu \frac{E_M}{E_b}) \quad (14)$$

3. 2 Calculation of Curie temperature

Based on the size-and-shape dependent model of cohesive energy, the Curie temperature of ferromagnetic nanoparticles can be further deduced. Considering that the Curie temperature is proportional to the cohesive energy, it is reliable to express the Curie temperature of

nanoparticles with both size and shape dependence as

For freestanding nanoparticles:

$$\frac{T_{Cn}}{T_{Cb}} = 1 - \frac{6\mu}{n^{1/3} C^{2/3} \pi k^2} \quad (15)$$

For embedded nanoparticles:

$$\frac{T_{Cn}}{T_{Cb}} = 1 - \frac{3\mu}{n^{1/3} C^{2/3} \pi k^2} \left(1 - \mu \frac{T_{CM}}{T_{Cb}}\right) \quad (16)$$

From the above expressions of Curie temperature in Eqns.(15) and (16), it is obvious that when the atoms that constitute a nanoparticle are determined, the parameters C and k are fixed. Then the Curie temperature of the nanoparticle is strongly dependent on its shape factor and atomic number. Here the atomic number can be regarded as one index of particle size, as it is natural that more atoms lead to larger size of nanoparticles. The values of shape factor for nanoparticles in different shape can be calculated according to their geometric characters and the definition in Eqn.(12). Calculation results for some typical shapes are listed in Table 1. Accordingly, it's safe to say that the Curie temperature of a nanoparticle depends on its size and shape effects, as well as its cohesive energy.

Table 1 Values of shape factor μ for nanoparticles

Shape	Shape factor μ
Cube	1
Sphere	0.806 0
Octahedron	0.953 2
Pentagonal decahedron	1.011 0
Regular tetrahedron	1.049 1
Ellipsoid, Cylinder, Six-edge column	≥ 0.806 0
Tetragonal, Rhombohedral	≥ 1

Meanwhile, comparison between Eqns.(15) and (16) suggests that the size and shape effects for freestanding nanoparticles will be more remarkable than those for embedded ones, as the latter depends on more variables in Eqn.(16). This phenomenon can be partly explained in the way that the freestanding materials have a larger surface-to-volume atomic ratio, so that their size and shape dependence is stronger than the embedded particles. For a certain nanoparticle, for example, freestanding Fe nanoparticles in cubic shape, the parameters μ , C , k and T_{Cb} in Eqn.(13) are 1, 2, $\sqrt{3}/4$ and 1 043 K, respectively. Then the relationship between the Curie temperature of nanoparticles and their atomic number can be plotted. Under different conditions, the parameters may change and the corresponding values of Curie temperature can be obtained.

3.3 Model validity and discussion

To validate the reliability of our model, the Curie

temperatures of ultrafine Fe, Co and Ni particles are numerically shown in Fig.1 with the reported experimental values. From Fig.1, it is clear that the Curie temperatures of ferromagnetic nanoparticles decrease with the decreasing size (described by the amount variation of atoms), which is in good accordance with the experimental observations mentioned before. The curves in Fig.1 are also compatible with the prediction by other theoretical models[7–8,12]. It is also interesting to find that the Curie temperature difference caused by shape effect becomes obvious only within a quite ultrafine size range, i.e. below 10 nm. Therefore, in a general situation, more emphases should be put on the size effect. Furthermore, compared the calculation curves with the available experimental data for Ni nanoparticles, it seems that the experiment data are well located in or between our prediction lines representing nanoparticles in cubic shape and spherical shape. Considering that the measured particles are approximating sphere together with other shapes, our prediction is in good accordance with the experimental data.

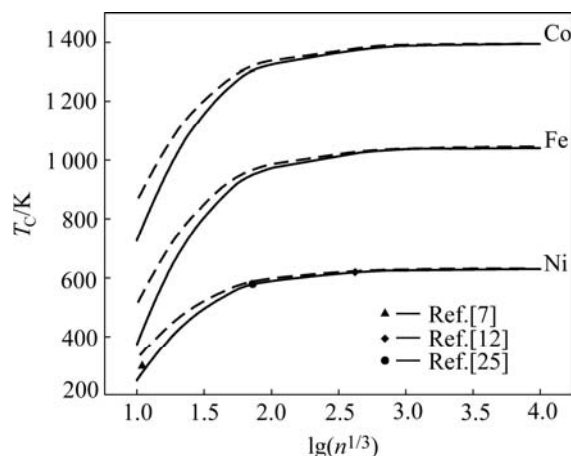


Fig.1 T_C function for freestanding Fe, C, Ni nanoparticles in terms of Eqn.(15) shown as solid lines for spherical shape and dash lines for cubic shape

For the systems of embedded nanoparticles, Curie temperature also depends on the interaction between the particle and substrate, together with the parameters mentioned above. When there is no or a weak interaction at the interface, the embedded nanoparticles may behave similarly to freestanding nanoparticles, namely the Curie temperature will decrease with the decreasing size. In case of a strong interaction or higher value of Curie temperature of the matrix (T_{CM} in Eqn.(16)), the Curie temperature of the embedded nanoparticle maybe change in an opposite way. Such phenomenon can also be explained in a view of energy variation. It has been reported that there exist different degrees of spin-spin interactions between inner and surface atoms, caused by the number reduction of spin interactions on the surface.

This will lead to a variation of lattice vibration. Therefore, when the size is decreased, the total energy, or the thermal vibration energy to disorder the ferromagnetic ordering state may change with the interaction conditions[26]. Until now, magnetic particles embedded in Ag or Cu matrix are two major types of particle-film giant magnetoresistance(GMR) materials in industry and research work. However, their Curie temperature variations for the embedded nanoparticles are not easily available at present. Eqn.(16) with parameters properly chosen will be helpful to be referred in theoretical investigation and practical production.

Furthermore, based on the definition of surface-to-volume atomic ratio α , there should be a direct relationship among the values of α for nanoparticles, nanowires and nanofilms with the same size R . For nanoparticles, R means the normal radius; for nanowires, R denotes the radius of the cross section; and for nanofilms, R represents the half value of the thickness. Accordingly, it can be deduced that for different low-dimensional systems, the surface-to-volume mole ratio is in the ratio of $\alpha_{\text{sphere}}:\alpha_{\text{film}}:\alpha_{\text{wire}}=3:2:1$, where α_{sphere} , α_{film} and α_{wire} are the surface-to-volume atomic ratio for nanoparticles, nanowires and nanofilms, respectively [16]. Then the above cohesive energy formulae and Curie temperature for particles can be extended to describe the properties of corresponding wires or films.

4 Conclusions

1) A simplified model is developed for the size-and-shape dependent Curie temperature of ferromagnetic nanoparticles, based on the relationship between the Curie temperature and cohesive energy.

2) The model predicts a decrease of Curie temperature with decreasing size of ferromagnetic nanoparticles. The shape of nanoparticles also plays an important role on the critical temperature variation within a quite ultrafine size range.

3) The simple model developed in this work agrees well with the available experimental data and other theoretical predictions.

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