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# Thermodynamic investigation of ZrO<sub>2</sub>-BaO system

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**Abstract:** Thermodynamic description of ZrO<sub>2</sub>-BaO system was developed using the available experimental information. Special attention was paid to the modelling of the perovskite phase BaZrO<sub>3</sub> by a temperature-dependent polynomial to fit the experimental thermodynamic properties. The liquid phases,  $C_{SS}$  (cubic ZrO<sub>2</sub> solid solution) and  $T_{SS}$  (tetragonal ZrO<sub>2</sub> solid solution) were modelled with Redlich-Kister formula. The compounds Ba<sub>2</sub>ZrO<sub>4</sub> and Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> were treated as stoichiometric phases and the BaO<sub>SS</sub> and M<sub>SS</sub> (halite BaO and monoclinic ZrO<sub>2</sub> solid solutions) were treated as pure compounds. Comparisons between the calculated and the measured phase diagram as well as the thermodynamic quantities indicate that the most reliable experimental information is satisfactorily accounted for by the present thermodynamic calculation.

Key words: ZrO2-BaO system; thermodynamic description; perovskite phase; Redlich-Kister formula

# **1** Introduction

Doped with certain amount of MgO, CaO, SrO, BaO,  $Y_2O_3$  or CeO<sub>2</sub>, the disruptive martensitic phase transformation of pure ZrO2 from monoclinic to tetragonal can be suppressed, thus the mechanical properties are greatly improved[1]. While the mechanical properties of partially stabilized zirconia(PSZ) or tetragonal zirconia polycrystals(TZP) with a smaller amount than needed to produce fully stabilized zirconia, are quite different from each other [2-4]. Obviously, the knowledge of the phase diagram and thermodynamic properties is of fundamental importance to define the processing conditions for making these materials and subsequent treatments to obtain optimal engineering properties. Associated with the sluggish kinetics at low temperatures, the formation of meta-stable phases, and the difficulties in conducting experiments at high temperatures, etc, the phase equilibria in ZrO<sub>2</sub>-included systems have been proved to be difficult to determine with certainty. Since only calorimetry, the electromotive force and mass spectrometry are practicable, measurements of the thermodynamic properties in ZrO<sub>2</sub>-included systems are also not easy from the experimental point of view. When the present investigation was initiated, the literature experimentally dealing with the ZrO<sub>2</sub>-BaO system gave an incomplete and confusing picture[5–8]. In this work, the Calphad technique was employed to determine the phase relations and thermodynamic properties in  $ZrO_2$ -BaO system with the aim to assess the thermodynamic properties of the various phases in the  $ZrO_2$ -BaO system and to provide the optimized thermodynamic parameters, which can reproduce the reliable experimental phase diagram, thermodynamic data and structural information satisfactorily.

# 2 Evaluation of experimental data in literature

#### 2.1 Phase diagram information

PASCHOAL et al[6] and SHEVCHENKO et al[7] were responsible for the major contributions to understanding the ZrO<sub>2</sub>-BaO liquidus phase diagram. By means of optical microscopy, X-ray diffraction(XRD) and differential thermal analysis(DTA) techniques, PASCHOAL et al[6] measured the liquidus in the BaO-rich side. Using the DTA method, SHEVCHENKO et al[7] constructed a series of the phase diagrams of ZrO<sub>2</sub>/HfO<sub>2</sub>-based systems, and the attention was paid to the ZrO<sub>2</sub>-rich side. The ZrO<sub>2</sub>-BaO liquidus equilibria reported by SHEVCHENKO et al[7] were in good agreement with those measured by WARTENBERG et al[8]. Based on the available experimental information, the ZrO<sub>2</sub>-BaO system was characterized by BaZrO<sub>3</sub> and

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 $Ba_2ZrO_4$  compounds, in which  $BaZrO_3$  melted congruently at (2 978±10) K, and  $Ba_2ZrO_4$  decomposed peritectically at about 2 600 K. The present work was mainly based on these experimental data to set up the liquidus equilibria, on the grounds that the high-purity specimens were employed, and experimental procedures were well described.

Both PASCHOAL et al[6] and SHEVCHENKO et al[7] did not report the compound  $Ba_3Zr_2O_7$ , while the available information on  $\{(1-x)(BaO)+x(ZrO_2)\}$ indicated the existence of Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> in the ZrO<sub>2</sub>-BaO system[8-9] and the phase diagram calculated by DASH et al[10] for  $\{(1-x_1-x_2)(Ba)+x_1(Zr)+x_2(O)\}$  indicated that Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> co-existed with BaZrO<sub>3</sub> at 1 287 K. And more, Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> was really prepared by the reaction of  $BaCO_3(s)$  and  $ZrO_2(s)$  in the mole ratio of 3/2 in an 1 300 K for 400 h in dry air[10] and alumina boat at was found at 1 650 K[11]. Consequently, special attention was paid to the compound Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> in this work with the aim to understand the difference existing in Refs.[6-11].

The maximum solubility of BaO in c-ZrO<sub>2</sub> (cubic ZrO<sub>2</sub>) and t-ZrO<sub>2</sub> (tetragonal ZrO<sub>2</sub>) is 0.025 mol [7]. This small solubility of BaO in ZrO<sub>2</sub> benefits the mechanical properties of zirconia very much and the measured data [7] were used to evaluate the thermodynamic properties of C<sub>SS</sub> (cubic ZrO<sub>2</sub> solid solution) and T<sub>SS</sub> (tetragonal ZrO<sub>2</sub> solid solution). The very limited solubility of ZrO<sub>2</sub> in halite BaO (about 0.005 mol)[6–8] was ignored. No experimental data were reported for the solubility of BaO in m-ZrO<sub>2</sub> (monoclinic ZrO<sub>2</sub>).

#### 2.2 Structural and thermodynamic information

The structural behavior and the thermodynamic properties of the perovskite phase BaZrO<sub>3</sub> have been the subjects of many investigations associated with the technological application[12–19]. Using hightemperature X-ray diffractometry, MATHEWS et al[12] measured the cell parameters, unit-cell volumes and the coefficients of volume thermal expansion of the zirconia CaZrO<sub>3</sub>, SrZrO<sub>3</sub> and BaZrO<sub>3</sub> in the temperature range from 298 to 1 675 K. The linear variation of the unit-cell volume and the cell parameters without any discontinuity indicated that the compound BaZrO<sub>3</sub> did not take place any phase transition, and the structure of BaZrO<sub>3</sub> was cubic. Using electromotive force, JOCAB et al[13] reported the enthalpies of formation of both SrZrO<sub>3</sub> and BaZrO<sub>3</sub> from the component oxides in the temperature range from 960 to 1 210 K. Based on the slope of electromotive force, SrZrO<sub>3</sub> was detected to undergo a structural transformation at about 1 123 K, while no structural transformation was detected for the compound BaZrO<sub>3</sub>[13]. Because the experimental procedures were well controlled and the experimental results were generally consistent with each other [12-13], the structure of BaZrO<sub>3</sub> was treated as cubic in the whole temperature range.

Several groups[13-19] investigated the thermodynamic properties of BaZrO<sub>3</sub>. Using high-temperature differential calorimeter, NAGARAJAN et al[14] reported the enthalpy increments H(T)-H(298) for BaZrO<sub>3</sub> from 1 000 to 1 700 K. Drop calorimetry was used by LEVITSKII[15], for H(T)-H(298) measurements on BaZrO<sub>3</sub>, respectively. BANERJEE et al[16] determined H(T)-H(298) of BaZrO<sub>3</sub> by a precise high-temperature Calvet micro- calorimeter in the temperature range from 365.7 to 981 K. CORDFUNKE et al[17] also reported the enthalpy values for BaZrO<sub>3</sub> in their compilations. GOSPODINOV et al[18] reported enthalpy data for BaZrO<sub>3</sub> in the temperature range between 298 and 500 K differential scanning calorimeter(DSC). These bv experimental data[14-16] except those of Ref.[18] were in good agreement with each other and join smoothly with the adiabatic measurements carried out by KING et al[19]. They were used to evaluate the Gibbs energy of BaZrO<sub>3</sub>. Data from GOSPODINOV et al[18] were too high to have any physical meaning and were excluded in this work. The estimated data from CORDFUNKE et al[17] were not adopted, since they were directly connected with the thermodynamic parameters.

The estimated thermodynamic properties at 298 K, i.e. the enthalpy of formation of BaZrO<sub>3</sub>  $\Delta_{\rm f}H(298)$ = (-1 768.58±2) kJ/mol[13,15], the molar heat capacity  $C_p(298)$ =(101.71±0.31) J/(mol·K)[19] and the standard entropy  $S^{\Theta}(298)$ =(124.7±2) J/(mol·K)[19] were adopted so that the evaluation can be carried out practically, but a low weight factor was applied to them.

The Gibbs energies of formation of BaZrO<sub>3</sub> relative to the pure oxides in the temperature range from 960 to 1 210 K, and from 1 180 to 1 320 K were determined by JOCAB et al[13] and LEVITSKII[15] using electromotive force, respectively. JOCAB et al[13] also reported the enthalpies of formation of BaZrO<sub>3</sub> from the component oxides in the temperature range from 960 to 1 210 K, which were in good agreement with the value at 1 060 K reported by MUROMACHI et al[20]. These data were not used in the optimization. However, they were compared with the calculated results in order to check the final modelling.

For the compounds  $Ba_2ZrO_4$  and  $Ba_3Zr_2O_7$ , the enthalpies of formation from the component oxides at 298 K were determined[11, 21]. These data were adopted to optimize the parameters of the compounds.

All temperatures quoted in this work were converted into the International Temperature Scale of 1990[22]. The thermodynamic functions were calculated at the normal constant pressure.

### **3** Thermodynamic models

The Gibbs energy function  $G_{\Phi,i}^{\Theta}(T) = G_{\Phi,i}(T) - H_i^{\Theta}$  for the component *i* (*i*=ZrO<sub>2</sub>, BaO) in the phase  $\Phi$  is expressed by

$$G_{\Phi,i}^{\Theta} = a + bT + cT \ln T + dT^{2} + eT^{-1} + fT^{3} + gT^{7} + hT^{-9}$$
(1)

where  $H_i^{\Theta}$  is the molar enthalpy of the component *i* at 298.15 K and 101 325 Pa in its standard element reference state, and *T* is the absolute temperature. The last two terms in Eqn.(1) are used only outside the ranges of stability, the term  $gT^7$  is relative to the liquid below the melting point and  $hT^{-9}$  to the solid phases above the melting point.

In the present work, the Gibbs energy functions of pure ZrO<sub>2</sub>,  $G_1^{\Theta}(ZrO_2)$ ,  $G_c^{\Theta}(ZrO_2)$ ,  $G_t^{\Theta}(ZrO_2)$  and  $G_m^{\Theta}(ZrO_2)$ , were taken from the assessments of DU et al[23]. The Gibbs energy functions of BaO,  $G_1^{\Theta}(BaO)$  and  $G_h^{\Theta}(BaO)$  were consistent with those used by LU et al[24], which were little different from those of SGTE substance database since some modification was made. Here, I denotes liquid, c, t and m stand for cubic, tetragonal and monoclinic ZrO<sub>2</sub>, respectively, h represents halite BaO. The Gibbs energy functions employed in this work are expressed as

$$G_{1}^{\Theta}(\text{ZrO}_{2}) = \begin{cases} -1\,040\,370 + 382.690\,4\,T - 67.506\,T\ln T - \\ 0.004\,913\,3\,T^{2} + 635\,630T^{-1} + \\ 2.978 \times 10^{-22}\,T^{7} & (298\,\text{K} \leqslant T \leqslant 2\,983\,\text{K}) \\ -1\,060\,705.8 + 538.008\,T - 87.864\,T\ln T \\ (2\,983\,\text{K} \leqslant T \leqslant 6\,000\,\text{K}) \end{cases}$$

$$G_{\rm c}^{\Theta}({\rm ZrO}_2) = \begin{cases} -1125\,234.1 + 496.722\,62\,T - 80\,T\ln T \\ (298\,{\rm K} \le T \le 2\,983\,{\rm K}) \\ -1151\,298.9 + 568.290\,43\,T - \\ 87.864\,T\ln T + 4.874\,54 \times 10^{33}\,T^{-9} \\ (2\,983\,{\rm K} \le T \le 6\,000\,{\rm K}) \end{cases}$$

(3)

$$G_{t}^{\Theta}(\text{ZrO}_{2}) = \begin{cases} -1\ 124\ 404.1 + 495.897\ 73\ T - \\ 80.299\ 8\ T\ \ln\ T + 0.001\ 087\ 41\ T^{2} \\ (298\ K \leqslant T \leqslant 2\ 983\ K) \\ -1\ 161\ 302.3 + 571.873\ 37\ T - \\ 87.864\ T\ \ln\ T + 8.71 \times 10^{33}\ T^{-9} \\ (2\ 983\ K \leqslant T \leqslant 6\ 000\ K) \end{cases}$$
(4)

$$G_{\rm m}^{\Theta}(\text{ZrO}_{2}) = \begin{cases} -1125\,386.9 + 411.834\,91T - \\ 67.506\,3\,T\,\ln T - 0.004\,913\,34\,T^{2} + \\ 635\,630\,T^{-1} \\ (298\,\text{K} < T < 2\,983\,\text{K}) \quad (5) \\ -1\,139\,046.7 + 564.802\,49\,T - \\ 87.864\,T\,\ln T - 5.462\,42 \times 10^{33}T^{-9} \\ (2\,983\,\text{K} \leqslant T \leqslant 6\,000\,\text{K}) \end{cases} \quad (5)$$

$$G_{c}^{\Theta}(BaO) = G_{h}^{\Theta}(BaO) + 29\ 624.35$$

$$(298\ K \leq T \leq 3\ 000\ K)$$

$$G_{t}^{\Theta}(BaO) = G_{h}^{\Theta}(BaO) + 50\ 739.69$$
(8)

$$(298 \text{ K} \leqslant T \leqslant 3 \ 000 \text{ K}) \tag{9}$$

Due to the lack of experimental information, the Gibbs energies of the hypothetical meta-stable  $ZrO_2$  and BaO were expressed relative to those of their stable structures:

$$G_{c(t,m)}^{\Theta}(BaO) = G_{h}^{\Theta}(BaO) + A_{1} + B_{1}$$
(10)

$$G_{\rm h}^{\Theta}(\operatorname{ZrO}_2) = G_{\rm m}^{\Theta}(\operatorname{ZrO}_2) + A_2 + B_2$$
(11)

where the coefficients  $A_i$  and  $B_i$  (*i*=1, 2) are to be assessed by checking their influence on the calculated phase equilibria.

The liquid phase and solid solutions  $C_{SS}$  and  $T_{SS}$  were described by Redlich-Kister polynomials. The Gibbs energy for the liquid was expressed by

$$G_{l,m} - H^{\Theta} = (1 - x)G_{l}^{\Theta}(ZrO_{2}) + xG_{l}^{\Theta}(BaO) + RT$$
  

$$\cdot [x \ln x + (1 - x)\ln(1 - x)] + x(1 - x)[a_{0} + b_{0}T + (1 - 2x)(a_{1} + b_{1}T) + \cdots]$$
(12)

where  $H^{\Theta}$  is the abbreviation of  $(1-x)H^{\Theta}(\text{ZrO}_2) + xH^{\Theta}(\text{BaO})$ , *R* is the gas constant, and *x* is the molar fraction of BaO. The interactive parameters  $a_0$ ,  $b_0$ ,  $a_1$  and  $b_1$  are to be optimized. The C<sub>SS</sub> and T<sub>SS</sub> were described by an analogous equation. Due to the very limited solubility of ZrO<sub>2</sub> in halite BaO and BaO in m-ZrO<sub>2</sub>, the BaO<sub>SS</sub> (halite BaO solid solution) and M<sub>SS</sub> (monoclinic ZrO<sub>2</sub> solid solution) were treated as pure compounds in this work.

The compounds  $Ba_2ZrO_4$  and  $Ba_3Zr_2O_7$  were modelled as stoichiometric phases due to the very limited information. The Gibbs energy of  $Ba_2ZrO_4$  was given by

$$G^{\Theta}(\operatorname{Ba}_{2}\operatorname{ZrO}_{4}) = A_{3} + B_{3}T + 2G_{h}^{\Theta}(\operatorname{BaO}) + G_{m}^{\Theta}(\operatorname{ZrO}_{2})$$
(13)

where  $A_3$  and  $B_3$  are connected with the enthalpy and entropy of formation from pure oxides in solid state, which will be evaluated in the course of optimization. The analogous equation, Eqn.(14) can be written for the Gibbs energy of Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub>:

$$G_{\rm s}^{\Theta}(\mathrm{Ba}_{3}\mathrm{Zr}_{2}\mathrm{O}_{2}) = A_{4} + B_{4}T + 3G_{\rm h}^{\Theta}(\mathrm{BaO}) + 2G_{\rm m}^{\Theta}(\mathrm{ZrO}_{2})$$
(14)

Since there were experimental thermodynamic data for BaZrO<sub>3</sub> in a wide temperature range[12–19], it was preferable to express its Gibbs energies relative to the SER state, and the following equation was used:

$$G_{\rm s}^{\Theta}({\rm BaZrO}_2) = a_1 + b_1T + c_1T\ln T + d_1T^2 + e_1T^{-1} \quad (15)$$

where the coefficients  $c_1$ ,  $d_1$  and  $e_1$  can be evaluated mainly from the measured enthalpy increments[14–16].

#### **4** Optimization procedure

The Thermo-calc software package was used to optimize the thermodynamic parameters. The critically selected experimental data were employed with some certain weights, and the weights can be changed systematically until most of the experimental data were accounted for within the claimed uncertainty limits.

Optimization was started with the perovksite phase BaZrO<sub>3</sub>. By using the measured thermodynamic data [14–16] selected in the above section, the numerical values of the coefficients  $c_1$ ,  $d_1$  and  $e_1$  in Eqn.(15) describing the Gibbs energy function of BaZrO<sub>3</sub> could be critically evaluated. Once  $c_1$ ,  $d_1$  and  $e_1$  have been estimated, the coefficients  $a_1$  and  $b_1$  in Eqn.(15) could be

estimated from the reported heat capacity, entropy, and enthalpy of formation of  $BaZrO_3$  at 298 K[13, 19]. The obtained coefficients were subjected to further optimization, the calculated thermodynamic properties of  $BaZrO_3$  at 298 K were compared with the literature available data[13,15, 19–20] in Table 1.

**Table 1** Estimated thermodynamic properties of perovskitephase BaZrO3 at 298 K compared with measured values

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Data	$\Delta_{ m f}H/$	<i>S</i> /	$C_p/$
source	$(kJ \cdot mol^{-1})$	$(J \cdot mol^{-1} \cdot K^{-1})$	$(J \cdot mol^{-1} \cdot K^{-1})$
This work	-1 775.61	124.62	101.78
Ref.[19]	-1 768.58[13]	$124.7 \pm 2$	$101.71 \pm 0.31$

Since the liquidus has been measured over a wide composition and temperature region [6-8], the optimization for its thermodynamic parameters is very important to the successful description of the ZrO<sub>2</sub>-BaO system. And since there are not any independent data for the liquid phase, such as experimental enthalpy of the mixture, the C<sub>SS</sub>, T<sub>SS</sub> and Ba<sub>2</sub>ZrO<sub>4</sub> should be modelled to reproduce the liquidus throughout the system. In this case, a suitable number of the thermodynamic parameters for each phase was really important to the optimization. It was found that the parameters  $a_0, b_0, a_1$ and  $b_1$  in Eqn.(12) should be introduced to describe the properties of the liquid satisfactorily. For the C<sub>SS</sub> and T<sub>SS</sub> phases, the experimental data were few, so the regular substitutional parameters were introduced to describe the relative properties. The coefficients  $A_3$  and  $B_3$  in Eqn.(13), were used to describe the compounds  $Ba_2ZrO_4$ . With most of experimental data[5-8] reproduced quite well, special attention was paid to the compound Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> to check the possibility of its existence. Because there were not any phase diagram data about the compound Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub>, the estimated enthalpy of formation of Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> from the component oxides at 298 K[11] was used to optimize the coefficients  $A_4$  and  $B_4$  in Eqn.(14).

All the thermodynamic parameters were finally evaluated together and slight adjustments were made to give the best description of the system.

#### **5** Results and discussion

The present evaluated thermodynamic parameters of the ZrO<sub>2</sub>-BaO binary system are as follows:

The interaction parameters of liquid:

 $a_0 = -357 817.66, b_0 = 73.4$ 

 $a_1 = -282549.78, b_1 = 93.9$ 

The interaction parameters of the C<sub>SS</sub> phase:

*a*<sub>0</sub>=-104 672.96, *b*<sub>0</sub>=-8.4

The interaction parameters of the T<sub>SS</sub> phase:

 $a_0 = -94\ 433$ 

Gibbs energy of BaZrO<sub>3</sub>:

$$G_{\rm s}^{\Theta}({\rm BaZrO}_2) = -1\ 818\ 096.5 + 688.86\ T -$$

Gibbs energy of Ba<sub>2</sub>ZrO<sub>4</sub>:

$$G_{\rm s}^{\Theta}({\rm Ba}_{2}{\rm ZrO}_{4}) = -209\,954.8 + 15.9T + 2G_{\rm h}^{\Theta}({\rm BaO}) + G_{\rm m}^{\Theta}({\rm ZrO}_{2})$$

Gibbs energy of Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub>:

$$G_{\rm s}^{\Theta}({\rm Ba}_{3}{\rm Zr}_{2}{\rm O}_{7}) = -361924.9 + 30.3T + 3G_{\rm h}^{\Theta}({\rm BaO}) + 2G_{\rm m}^{\Theta}({\rm ZrO}_{2})$$

A comparison between the calculated ZrO<sub>2</sub>-BaO phase diagram and that measured by ADAMSON et al [5-8] is shown in Fig.1. The calculated invariant reaction temperatures are compared with the experimental ones[5–8] in Table 2. It can be seen from Table 2 that the present modelling can account for the measured invariant temperatures [5-8] quite well. The eutectoid reactions  $T_{SS} \longrightarrow M_{SS} + BaZrO_3$  at 1 454 K and the peritectiod reaction Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> Ba<sub>2</sub>ZrO<sub>4</sub>+BaZrO<sub>3</sub> at 1 650 K are the results of calculations. These reactions are not easy to be experimentally detected because of the following reasons: 1) it is not easy to detect Ba<sub>3</sub>Zr<sub>2</sub>O<sub>7</sub> from  $Ba_2ZrO_4$  or  $BaZrO_3$  due to the near composition; 2) it is very difficult for oxides to achieve equilibrium at a low temperature such as 1 454 K. Better knowledge on the phase equilibria at low temperatures is useful for further refinement of the ZrO<sub>2</sub>-BaO system.

In Fig.2, the calculated H(T)-H(298) for BaZrO<sub>3</sub> is compared with the experimental values[14–16]. The agreement between the calculated and measured values of H(T)-H(298) is acceptable within the experimental



**Fig.1** Comparison between calculated ZrO<sub>2</sub>-BaO phase diagram and experimental data in Refs.[5–8]

Table 2Comparison between calculated and measuredcoordinates of invariant temperatures in ZrO2-BaO system

	Invariant temperature/K			
Equilibrium	Ref.[5]	Ref.[6]	Ref.[7-8]	This work
$L + T_{SS} - C_{SS}$			2 553	2 535
L = T <sub>SS</sub> +BaZrO <sub>3</sub>			2 513	2 512
L → BaZrO <sub>3</sub>	2 978	2 978	2 893	2 993
$L+BaZrO_3 \Longrightarrow Ba_2ZrO_4$		$\approx 2~673$		2 621
L Ba <sub>2</sub> ZrO <sub>4</sub> +BaO <sub>SS</sub>		1 608		1 612
$BaZrO_3+Ba_2ZrO_4$				1 650
$\begin{array}{c} Ba_{3}Zr_{2}O_{7}\\ \hline T_{SS} \longrightarrow M_{SS} + BaZrO_{3} \end{array}$				1 454



**Fig.2** Comparison of calculated H(T)-H(298) of BaZrO<sub>3</sub> with measured data [14–16]

uncertainties.

The calculated Gibbs energy and enthalpy of formation for  $BaZrO_3$  from the pure oxides are compared with the experimental data[13, 15, 19–20] in Tables 3 and 4, respectively. The calculation can describe these experimental data reasonably although they are not used in the present optimization.

**Table 3** Gibbs energy of formation of BaZrO<sub>3</sub> from component oxides compared with measured values in Refs.[13, 15]

Tomporatura/V	$G/(kJ \cdot mol^{-1})$		
Temperature/K -	Ref.[13]	Ref.[15]	This work
1 000	-129.55	$-136.4\pm4$	-128.543
1 100	-129.73	$-136.6\pm4$	-128.573
1 200	-129.91	$-136.8 \pm 4$	-128.572

The present calculated enthalpy of formation for the compounds  $Ba_2ZrO_4$  and  $Ba_3Zr_2O_7$  from the component oxides at 298 K are compared with the literature data in Table 5, a good agreement is obtained.

**Table 4** Enthalpy of formation of BaZrO<sub>3</sub> from component oxides compared with measured values in Refs.[13, 20]

1	L / J		
Tomporatura/V	$H/(kJ \cdot mol^{-1})$		
Temperature/K	Ref.[13]	Ref.[20]	This work
298	$-125.56\pm2$		-126.93
1 085	$-127.76\pm2$		-128.23
1 060		$-123.9 \pm 4$	-128.28

Table 5 Comparison of enthalpy of formation for  $Ba_2ZrO_4$  and  $Ba_3Zr_2O_7$  from component oxides at 298 K

Common d	$H/(kJ \cdot mol^{-1})$		
Compound	Ref.[20]	This work	
$Ba_2ZrO_4$	$-2421.3\pm1$	-2 406.7	
Ba <sub>3</sub> Zr <sub>2</sub> O <sub>7</sub>	$-4204.3\pm5.7$	-4 207.4	

# **6** Conclusions

1) The thermodynamic function of the perovskite phase  $BaZrO_3$  is critically evaluated with all reliable experimental data reproduced within the estimated experimental uncertainty. A set of reasonable and self-consistent thermodynamic parameters for the  $ZrO_2$ -BaO binary system is obtained. The calculated phase diagram and thermodynamic properties data are in good correspondence with the experimental information.

2) The compound  $Ba_3Zr_2O_7$  decomposes to  $Ba_2ZrO_4$ and  $BaZrO_3$  at 1 650 K. Thermodynamic and phase diagram measurements on  $Ba_3Zr_2O_7$  are useful for further refinement of the compound and the  $ZrO_2$ -BaO system.

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